



Differentiable Robotics

Boris Ivanovic, Peter Karkus | American Control Conference 2023

NVIDIA Autonomous Vehicle Research Group

Members



Faculty Scientists



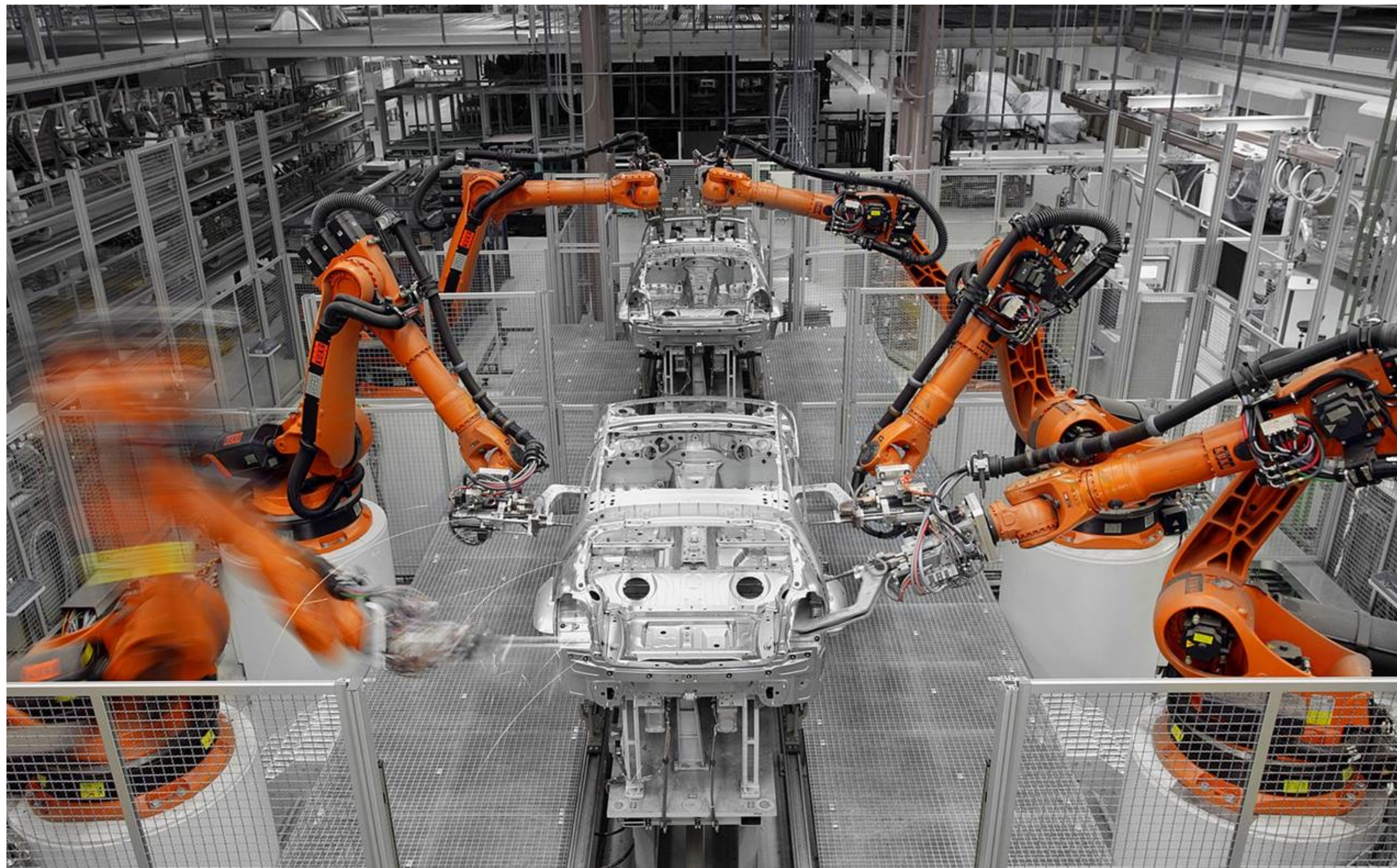
Consultant



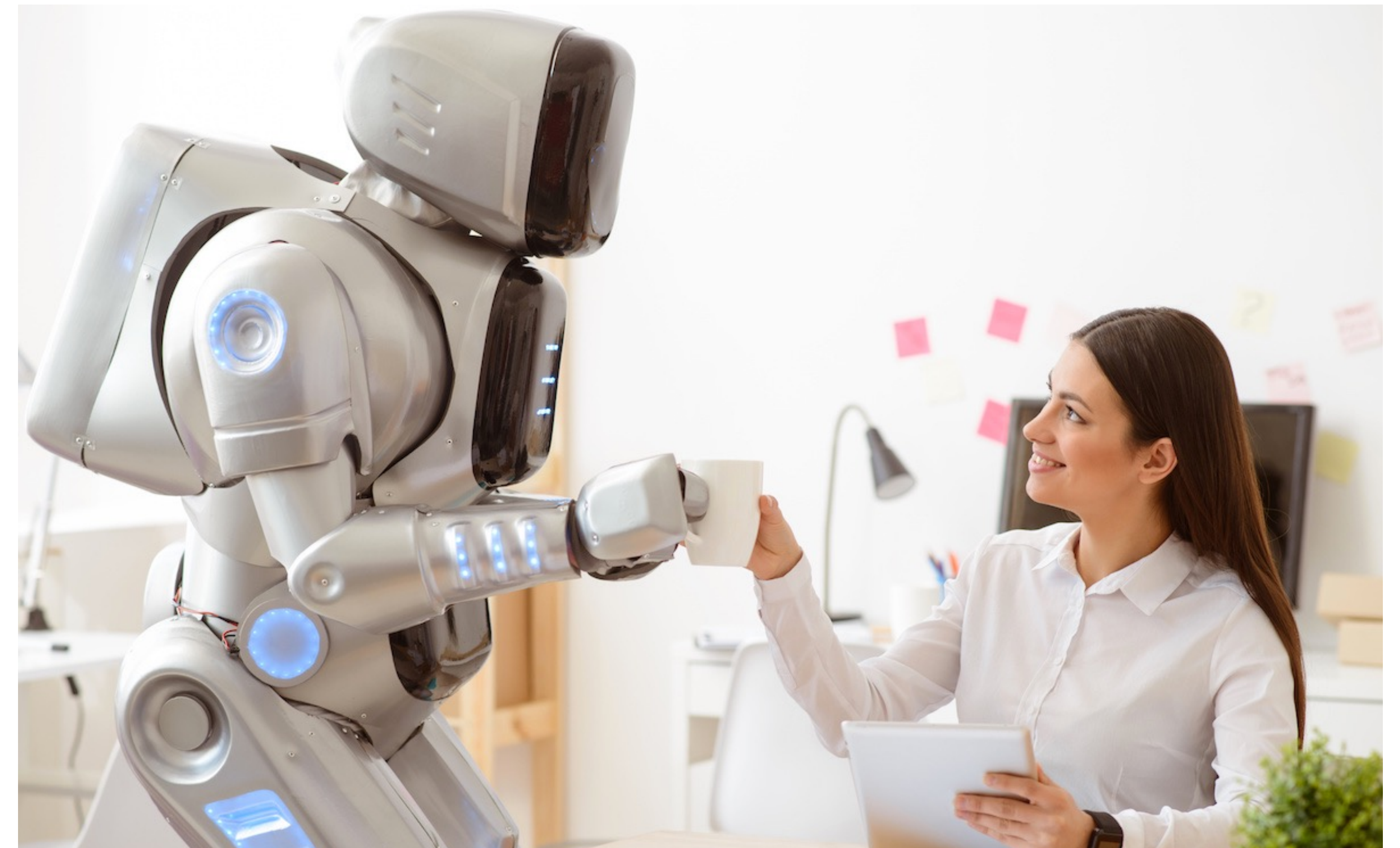
For more information about the Autonomous Vehicle Research Group:

<https://research.nvidia.com/labs/avg/>

From control to human-level robot intelligence



Robots today

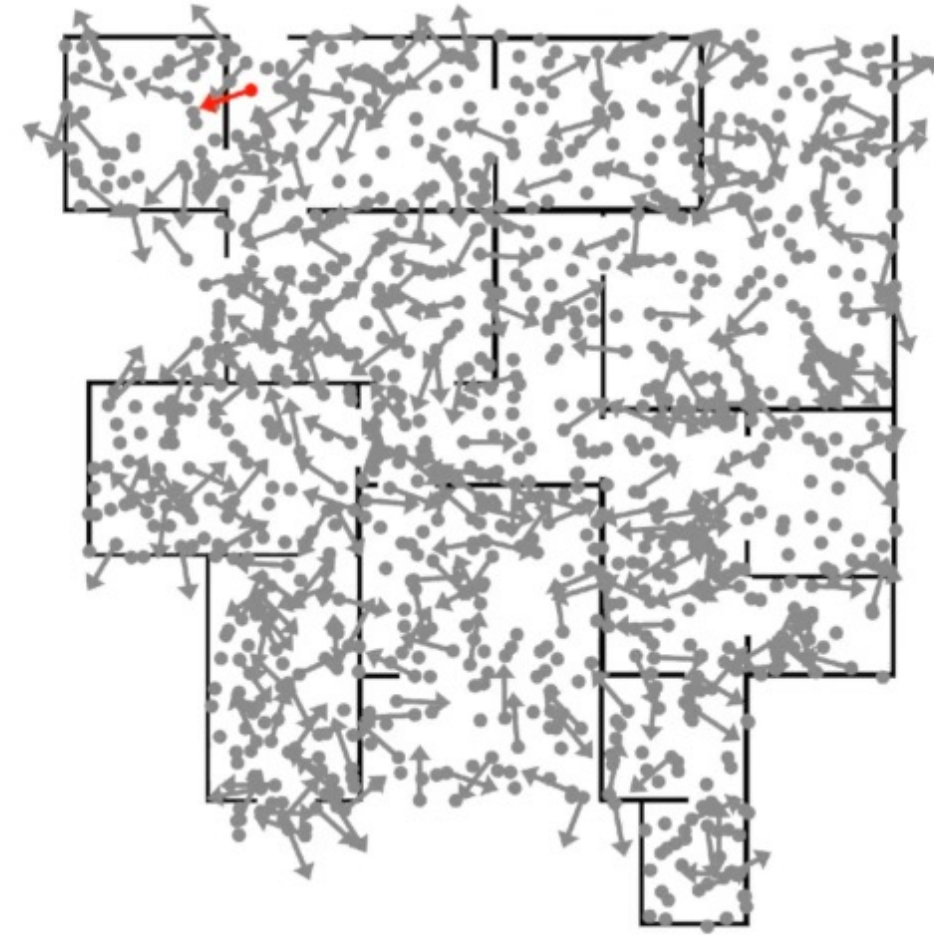


Robots tomorrow

Differentiable Algorithm Networks (DANs)

a general architecture for designing scalable and compositional robot learning systems.

Applications



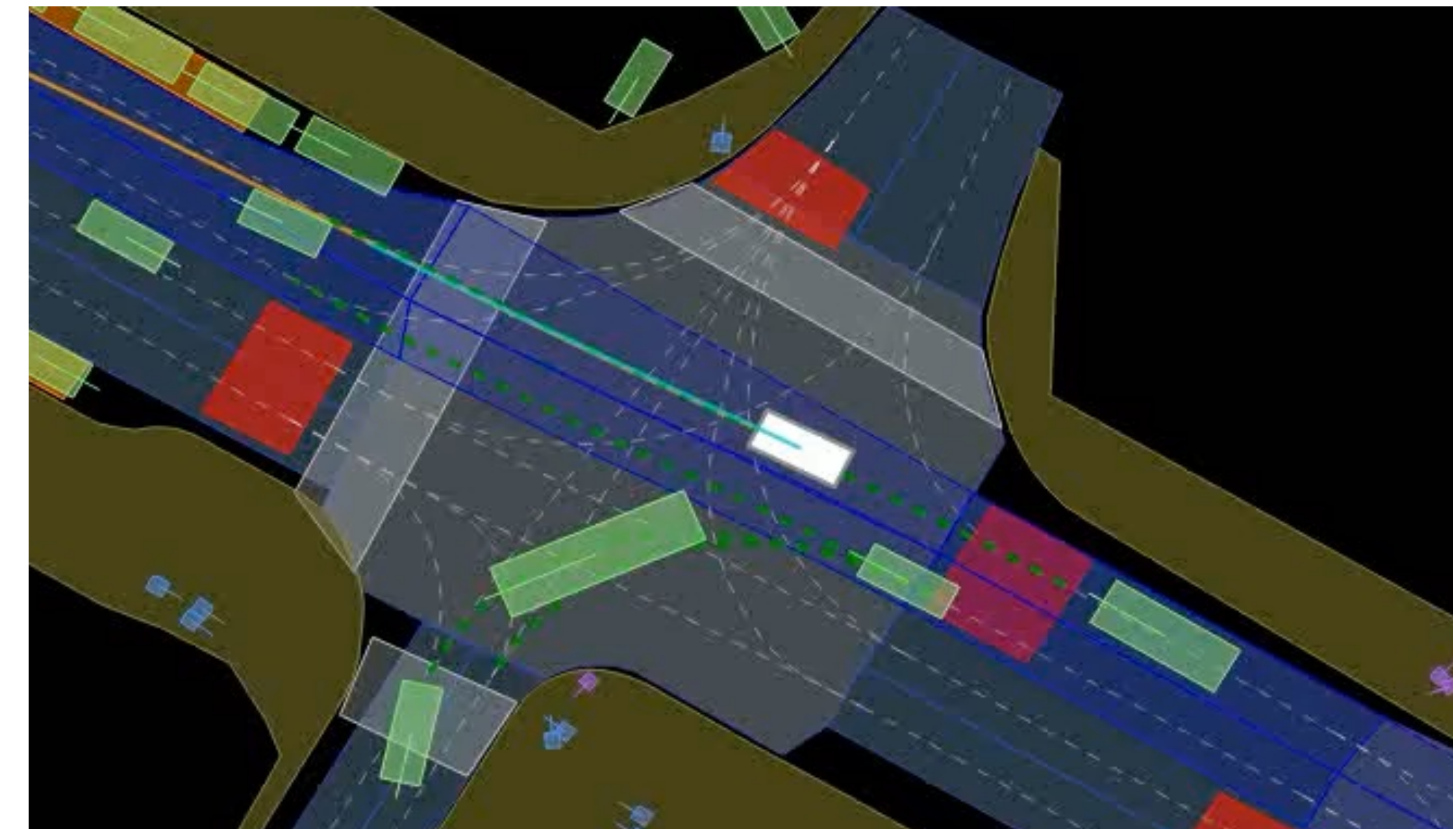
Visual localization



SLAM

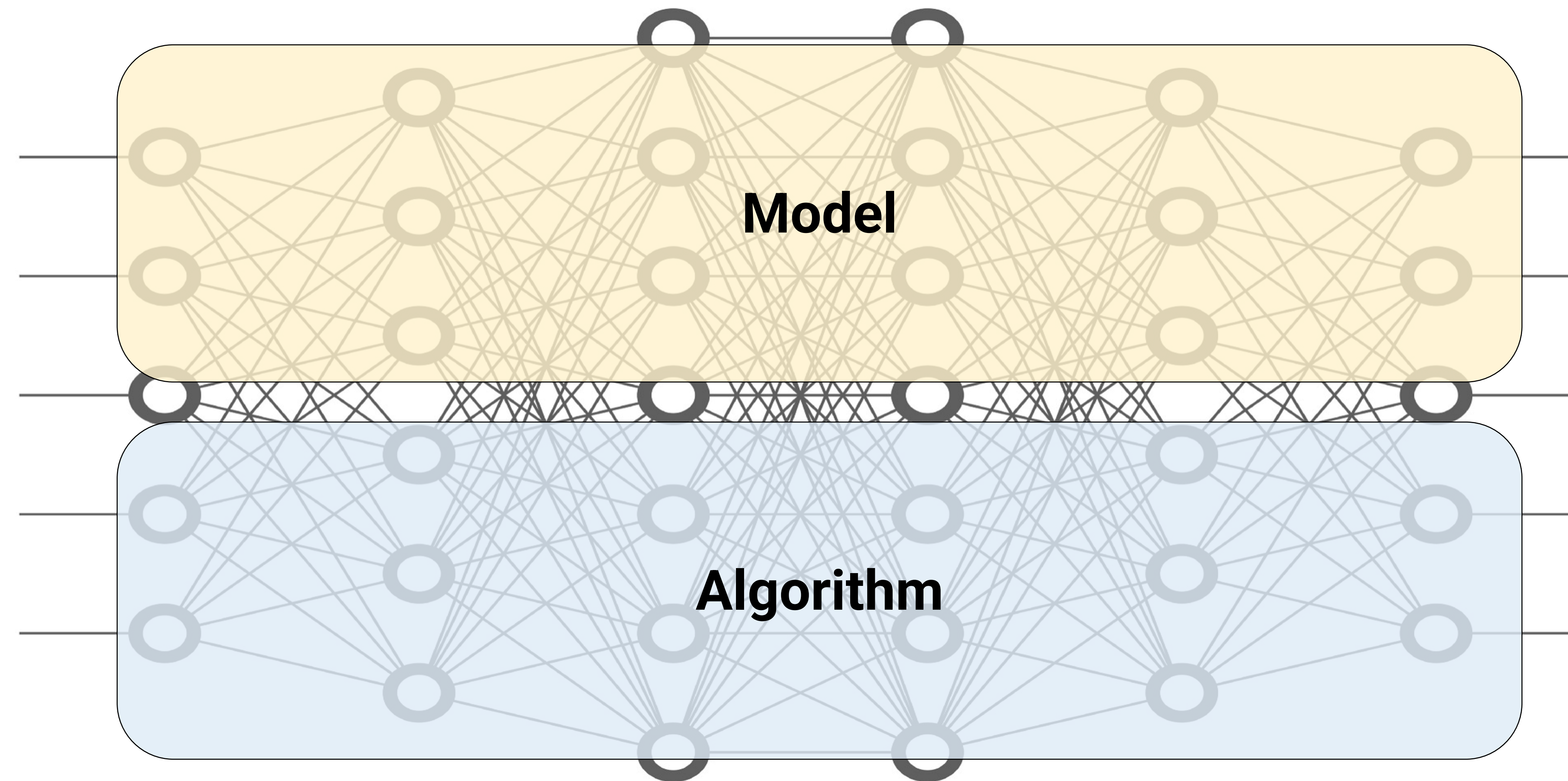


Navigation



Autonomous driving

Idea: encode algorithms in neural networks



Differential Neural Network = Computation graph

Example: value iteration

MDP:

$$S, A, T(s, a, s'), R(s, a)$$

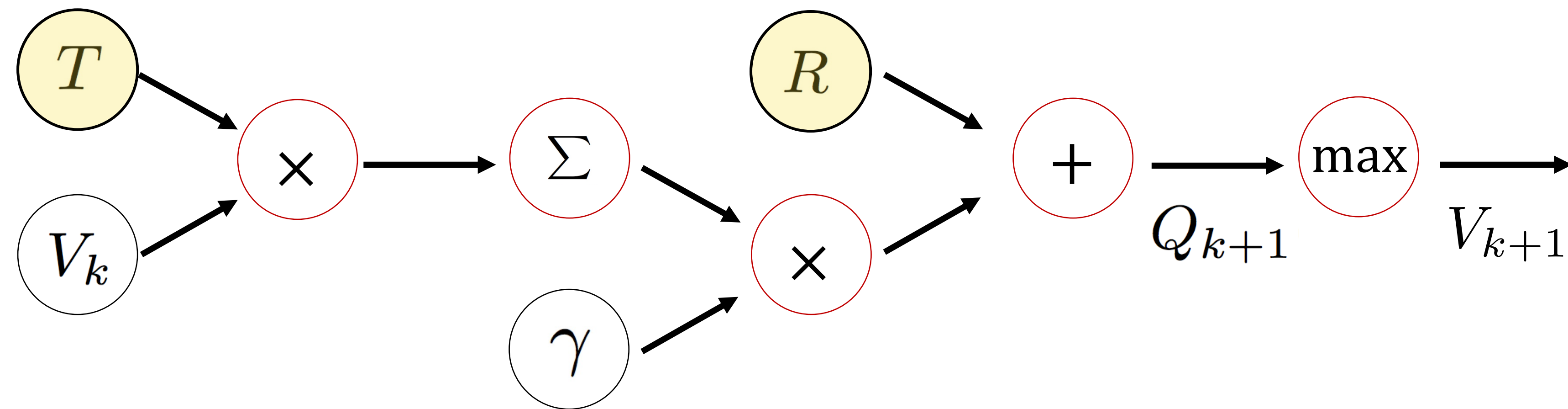
ValueIteration:

Repeat for $k = 1 : K$

$$Q_{k+1}(s, a) = R(s, a) + \gamma \sum_{s' \in S} T(s, a, s') V_k(s')$$

$$V_k(s) = \max_a Q_k(s, a)$$

$$a_t = \operatorname{argmax}_a Q_K(s_t, a)$$



Example: value iteration

MDP:

$S, A, T(s, a, s'), R(s, a)$

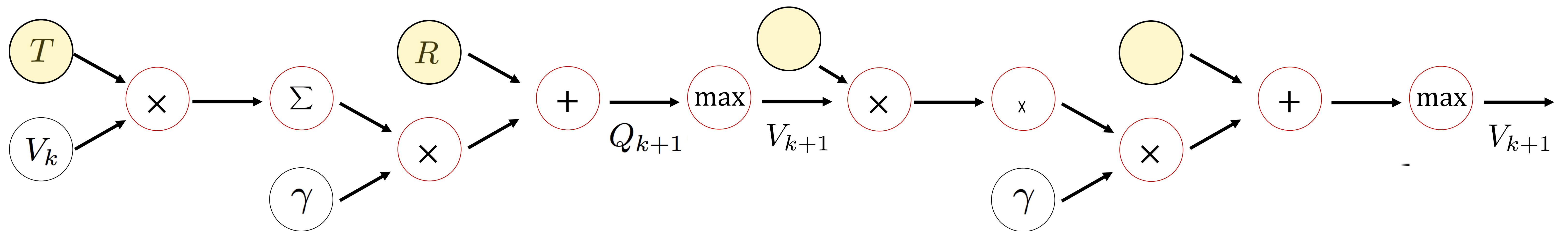
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Example: value iteration

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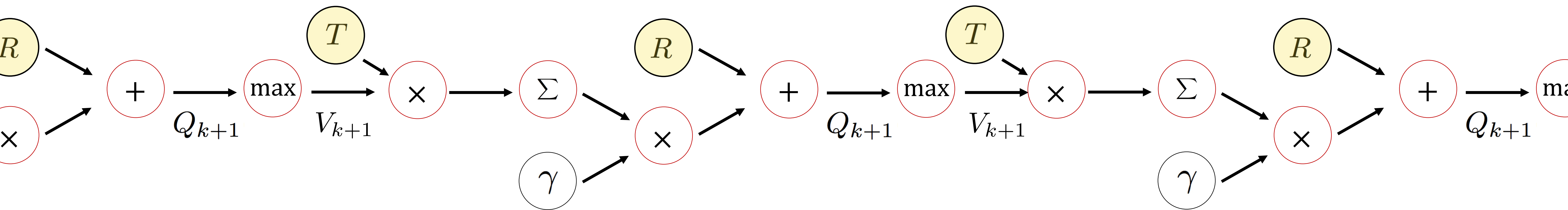
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Example: value iteration

MDP:

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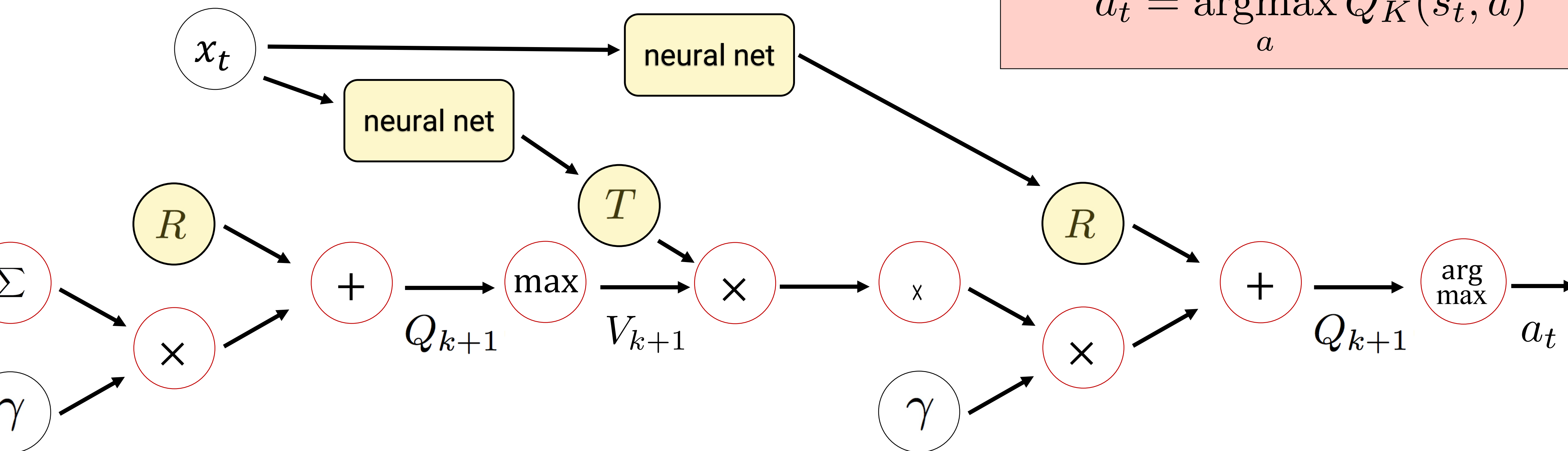
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Technical challenges

Non-differentiable operations

- Continuous relaxation
- Sampling
 - reparameterization trick
 - Gumbel-softmax
 - straight-through estimation
 - importance sampling
- Implicit gradients (e.g., ODEnet)
- Score-function estimation
(stochastic computation graphs)

Large computation graph

- Efficient parameterization
- Scale algorithm at test time
- Implicit gradients

State Estimation

Kalman filter

Haarnoja et al. 2016

Kloss et al. 2018

Histogram filter

Jonschkowski et al. 2016

Particle filter

Jonschkowski et al. 2018

Karkus et al. 2018

Wen et al. 2020

Mapping

Gupta et al. 2017

Karkus et al. 2020

SLAM

Jatavallabhula et al. 2019

Karkus et al. 2021

Planning

Value Iteration

Tamar et al. 2016

Shankar et al. 2016

Gupta et al. 2017

Lee et al. 2018

MCTS

Guez et al. 2018

QMDP planner

Karkus et al. 2017

Breadth-first search

Oh et al. 2017

Fraquhar et al. 2017

A* search

Yonetani et al. 2020

Control

Model-predictive control

Amos et al. 2018

East et al. 2020

Path-integral optimal control

Okada et al. 2017

ODE solver

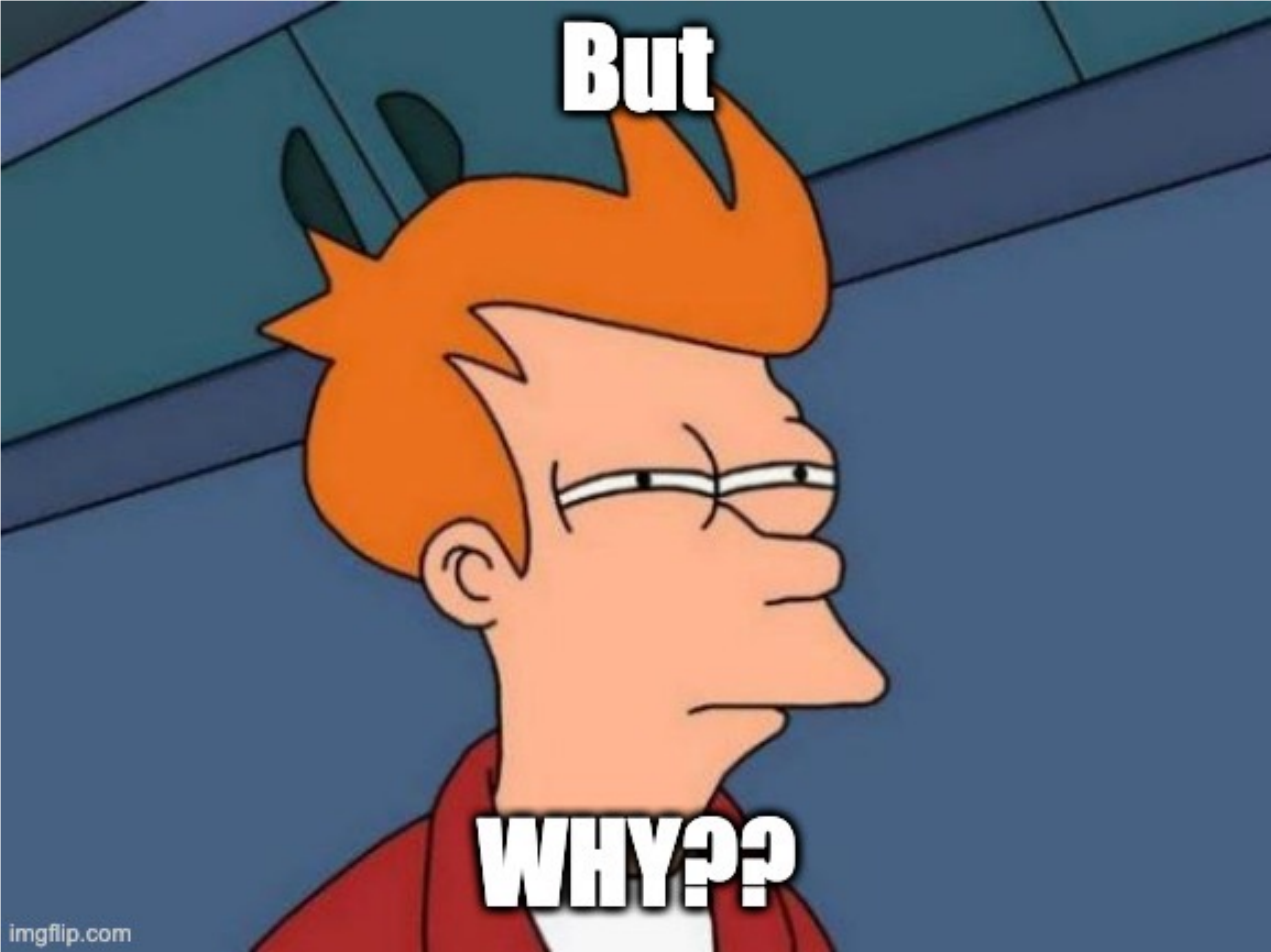
Chen et al. 2018

Zhong et al. 2020

Convex optimization

Amos et al. 2017

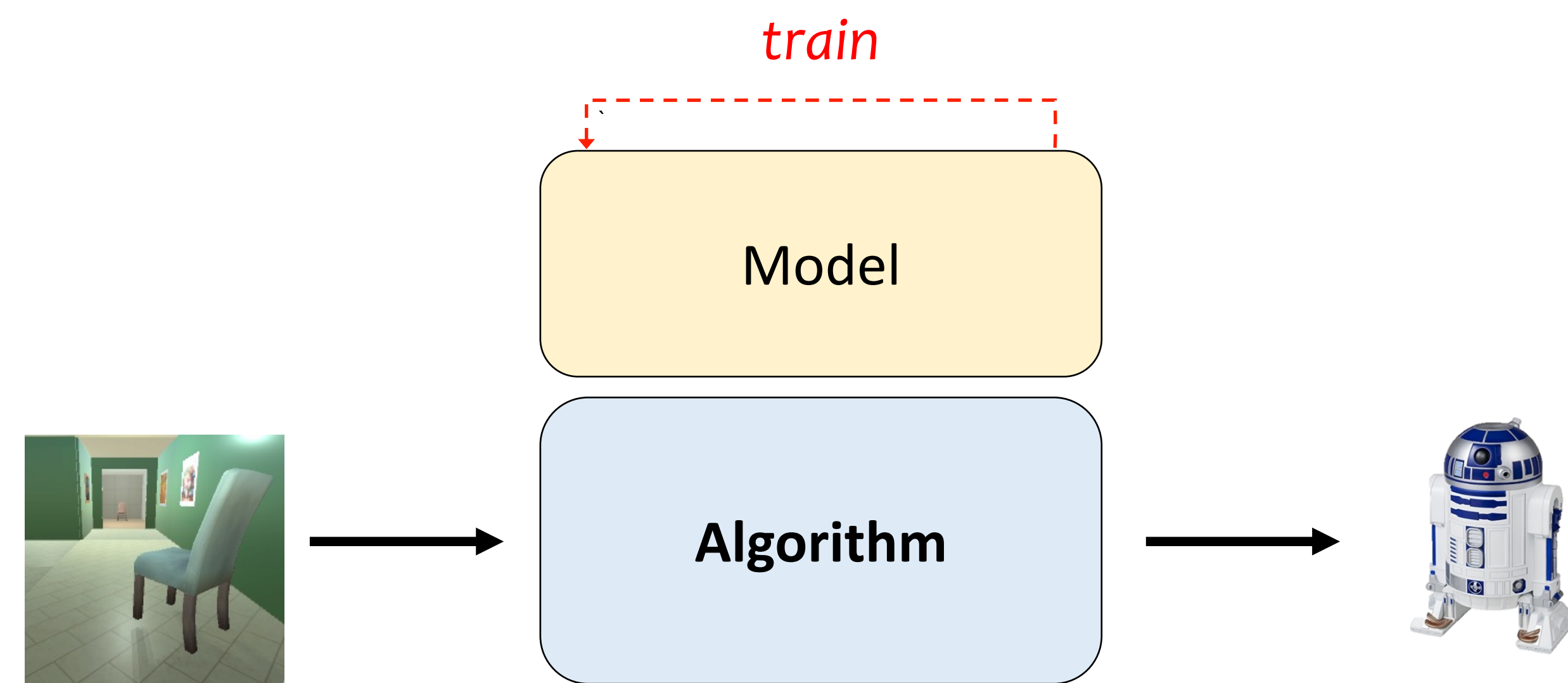
Agrawal et al. 2018



But

WHY???

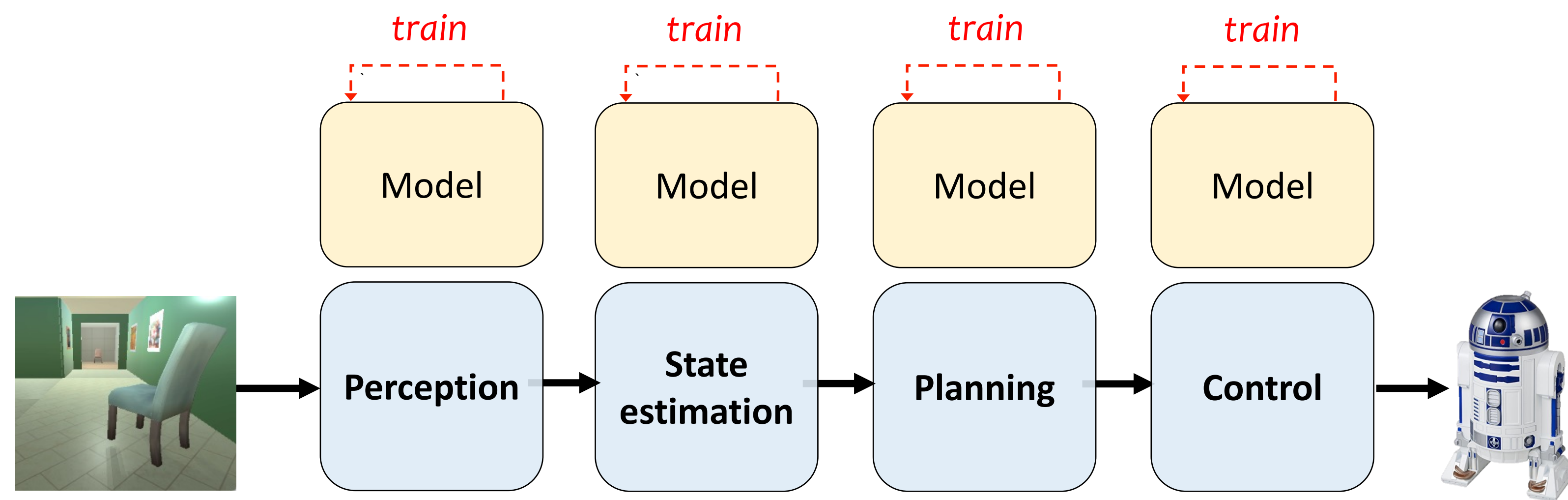
Model-based



Model-free

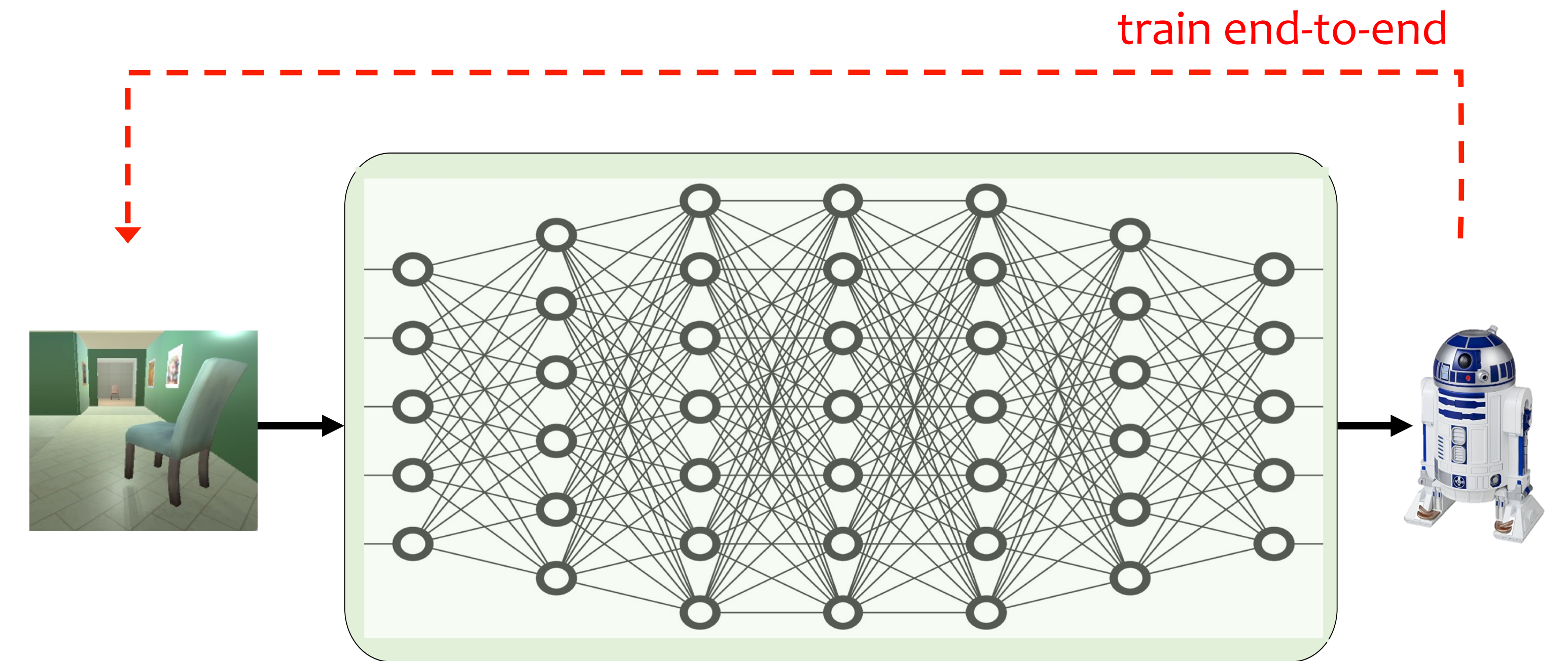


Model-based

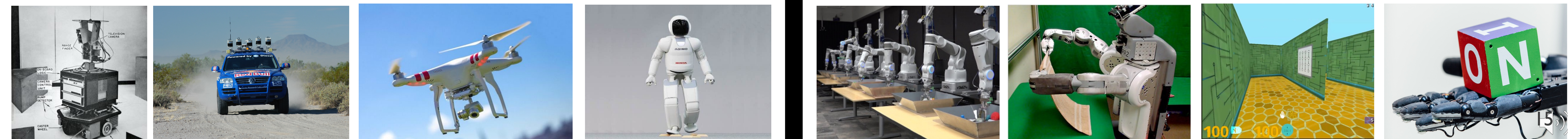


Composable and *interpretable* but *Brittle* because of unavoidable approximations.

Model-free



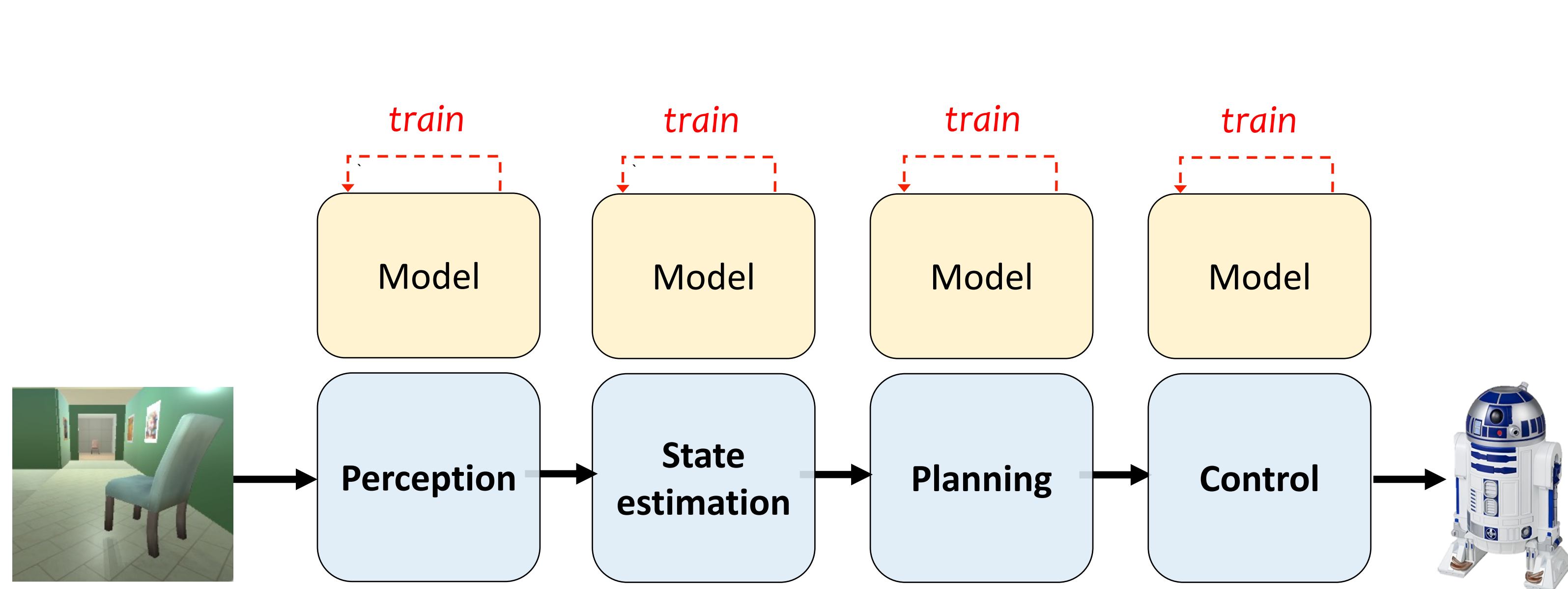
End-to-end learnable but *Lacks prior* for compositional generalization, and *interpretability* for safety guarantees



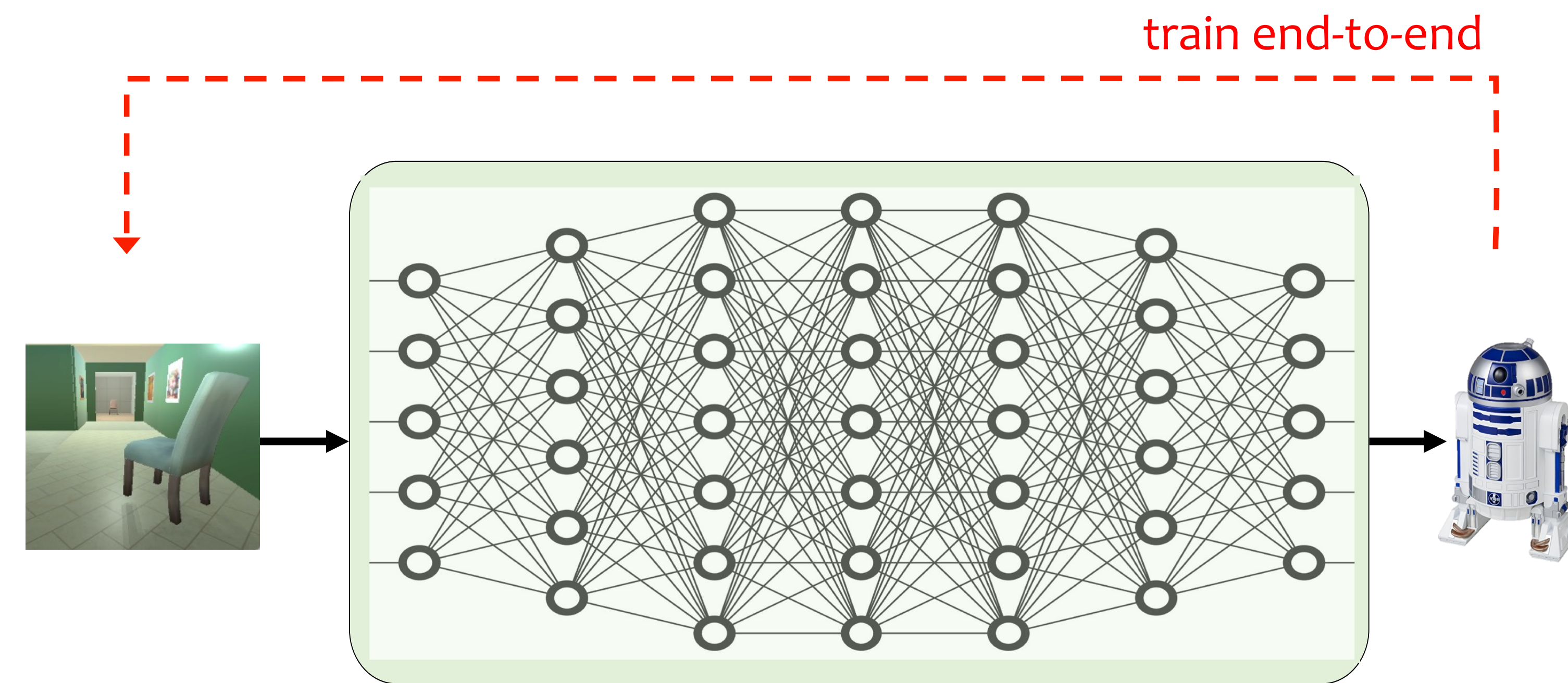
Model-based

+

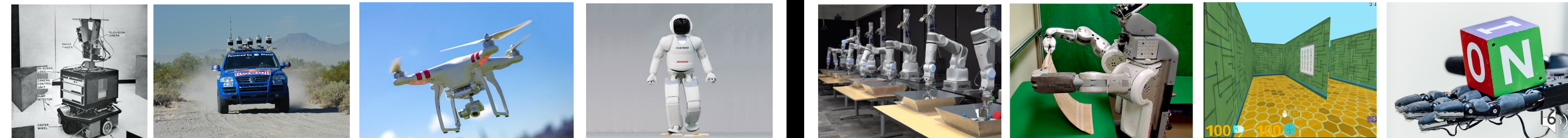
Model-free



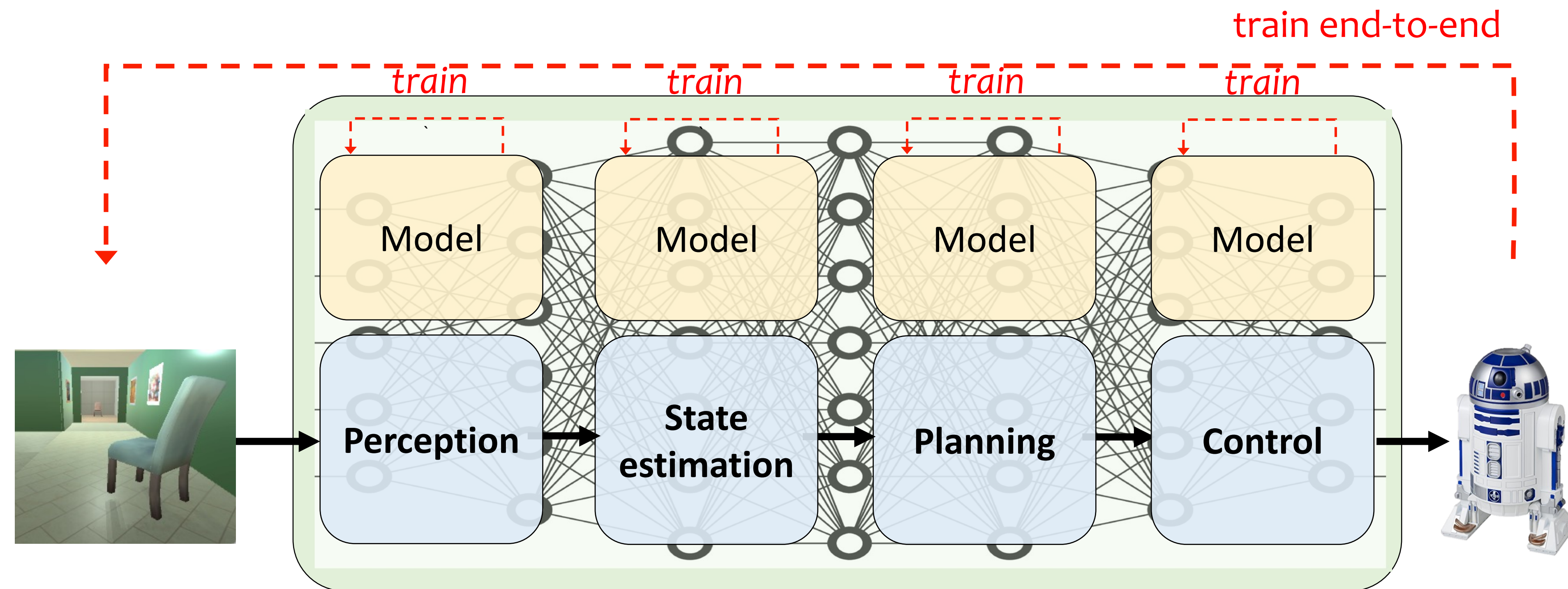
Composable but
Brittle because of unavoidable approximations



End-to-end learnable but
Lacks prior for compositional generalization and
interpretability for safety guarantees



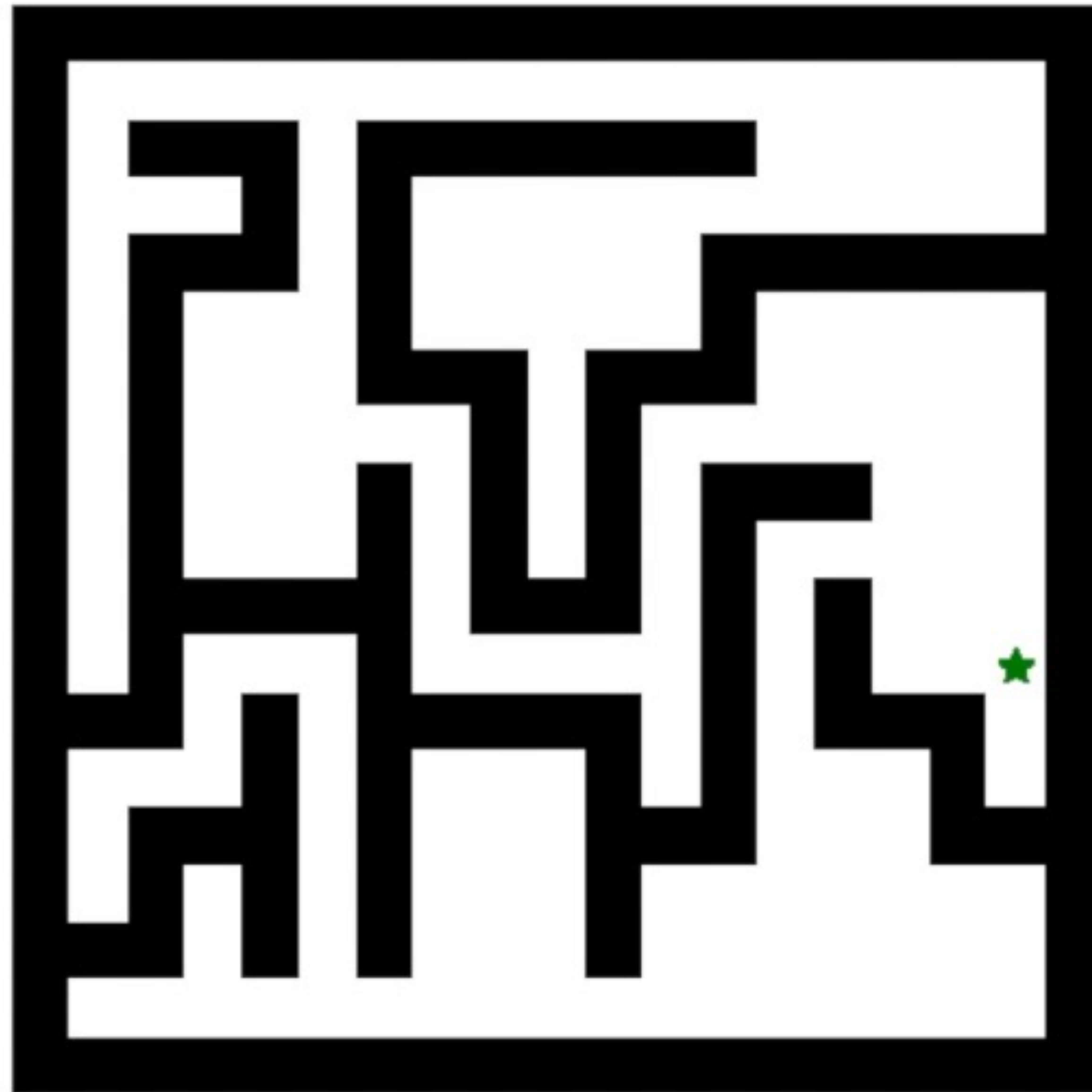
Modular + End-to-end



Differentiable Algorithm Network (DAN)

Case study: visual navigation

Map & Goal

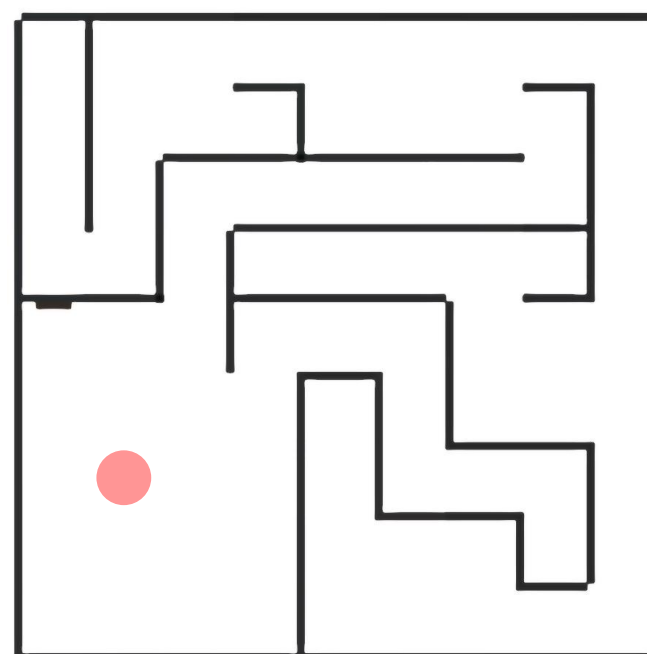
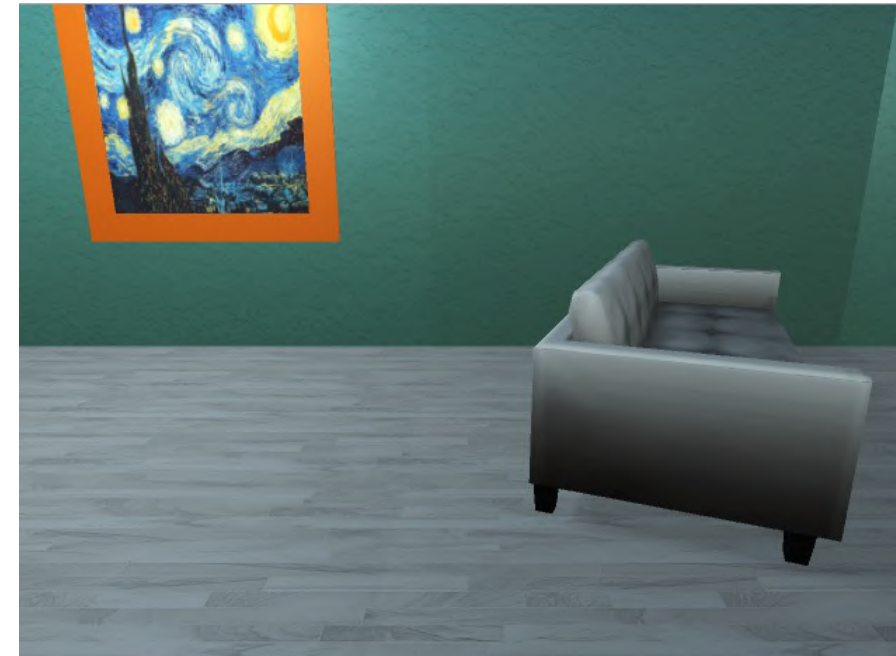
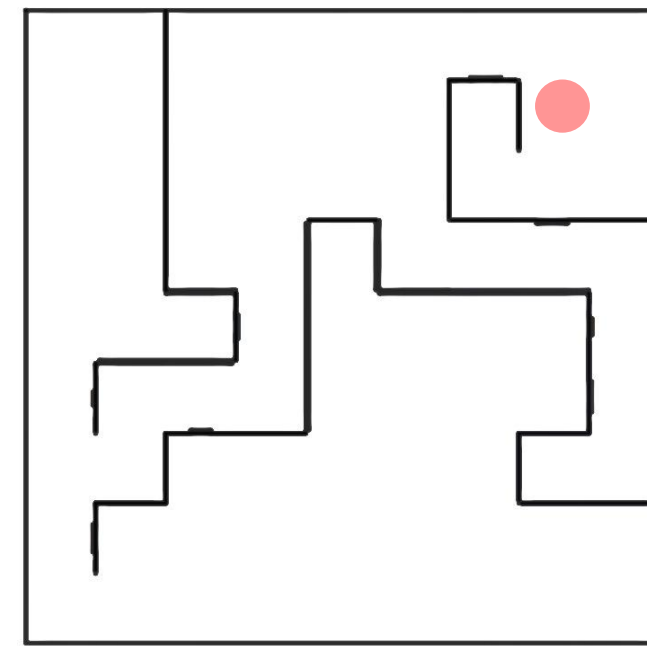


Observation

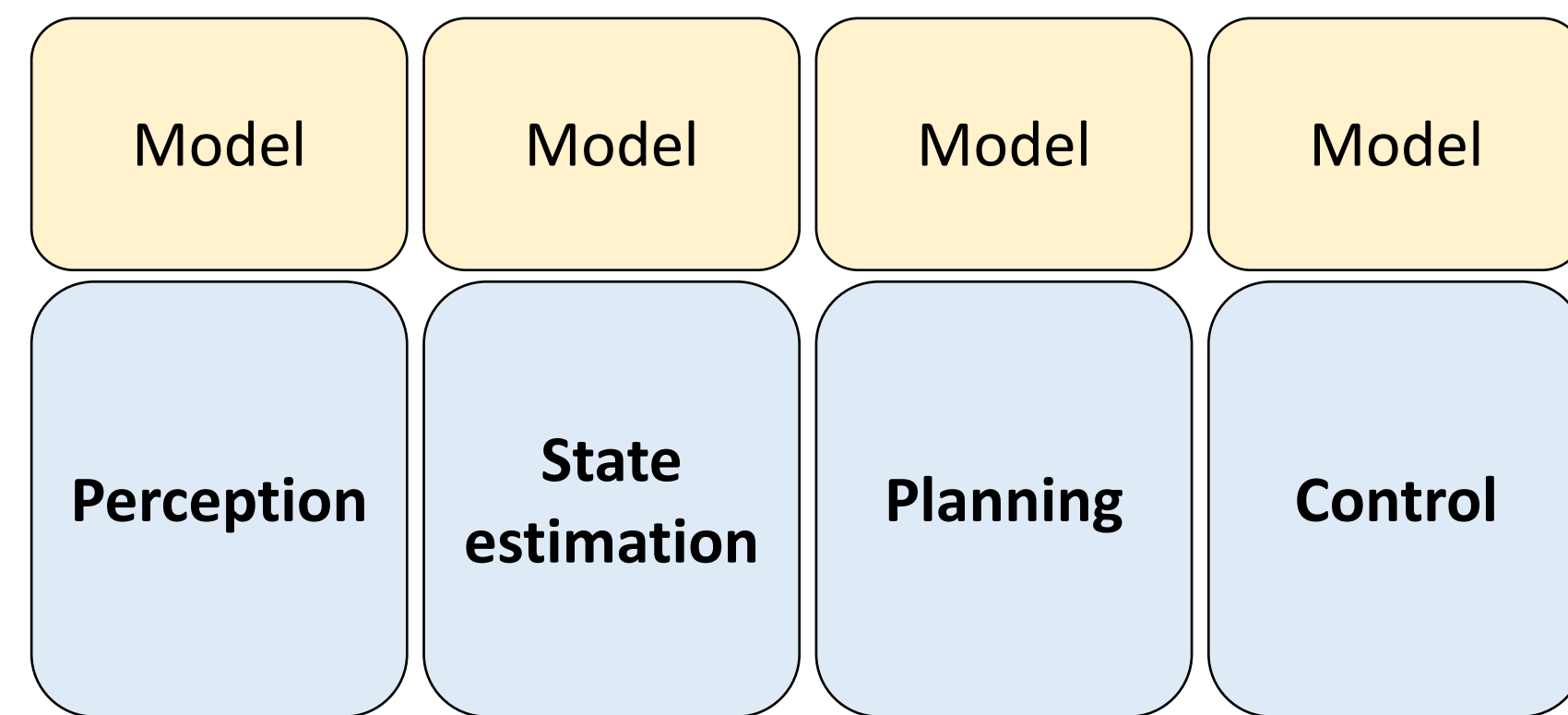


Case study: visual navigation

Train
10k expert demos

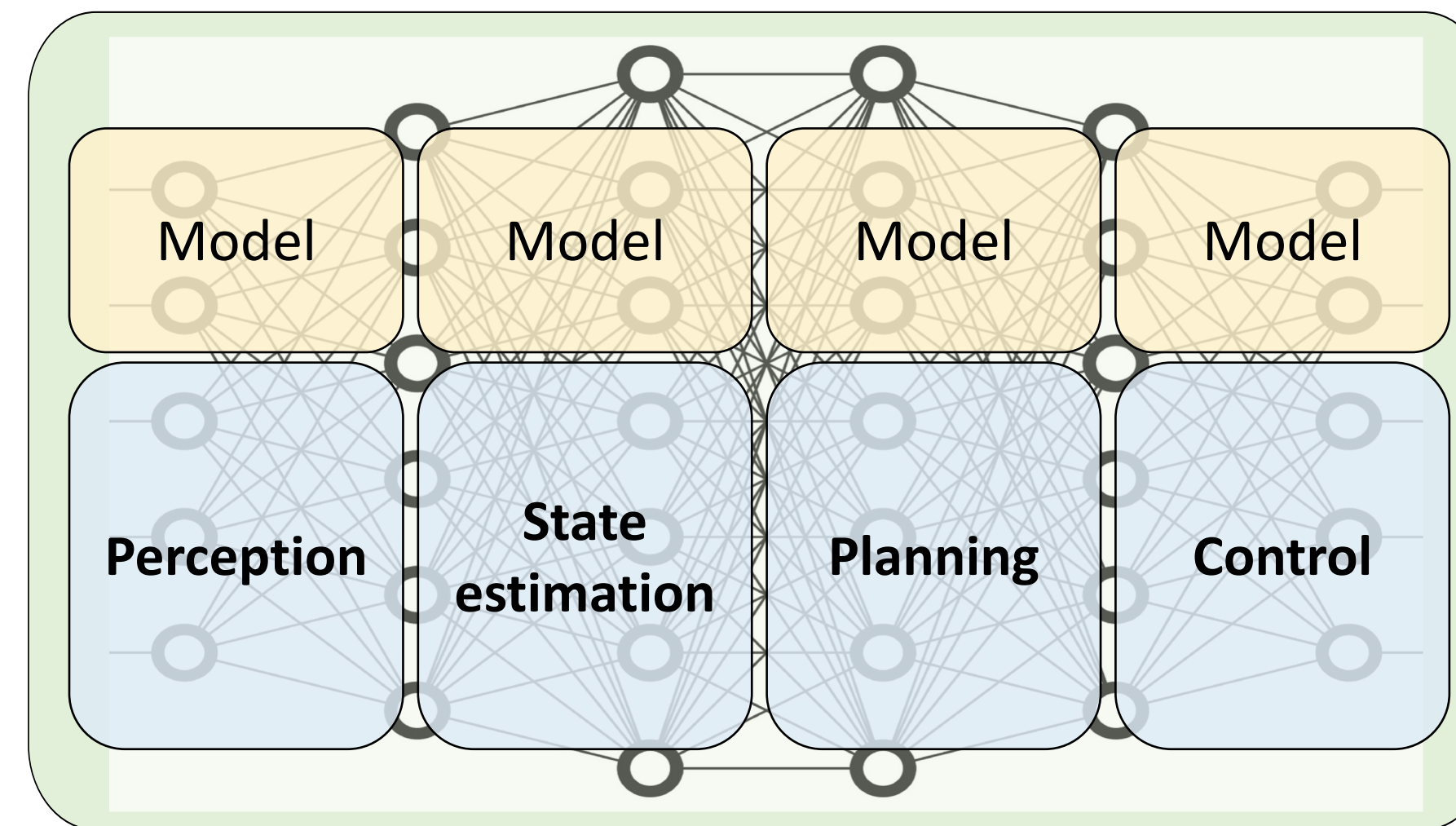


Modular



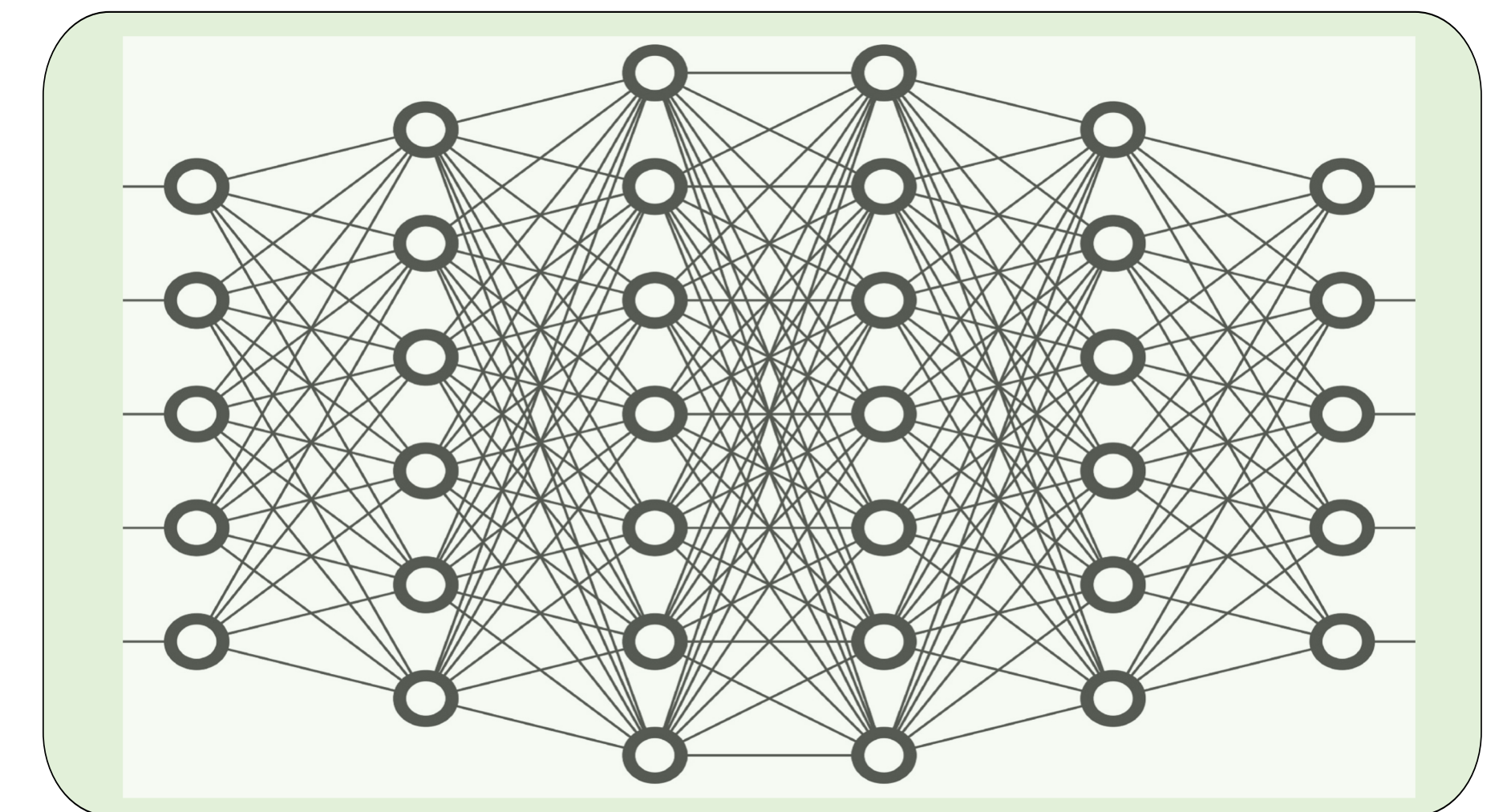
76.6%
success rate

DAN (ours)



99.8%
success rate

End-to-end

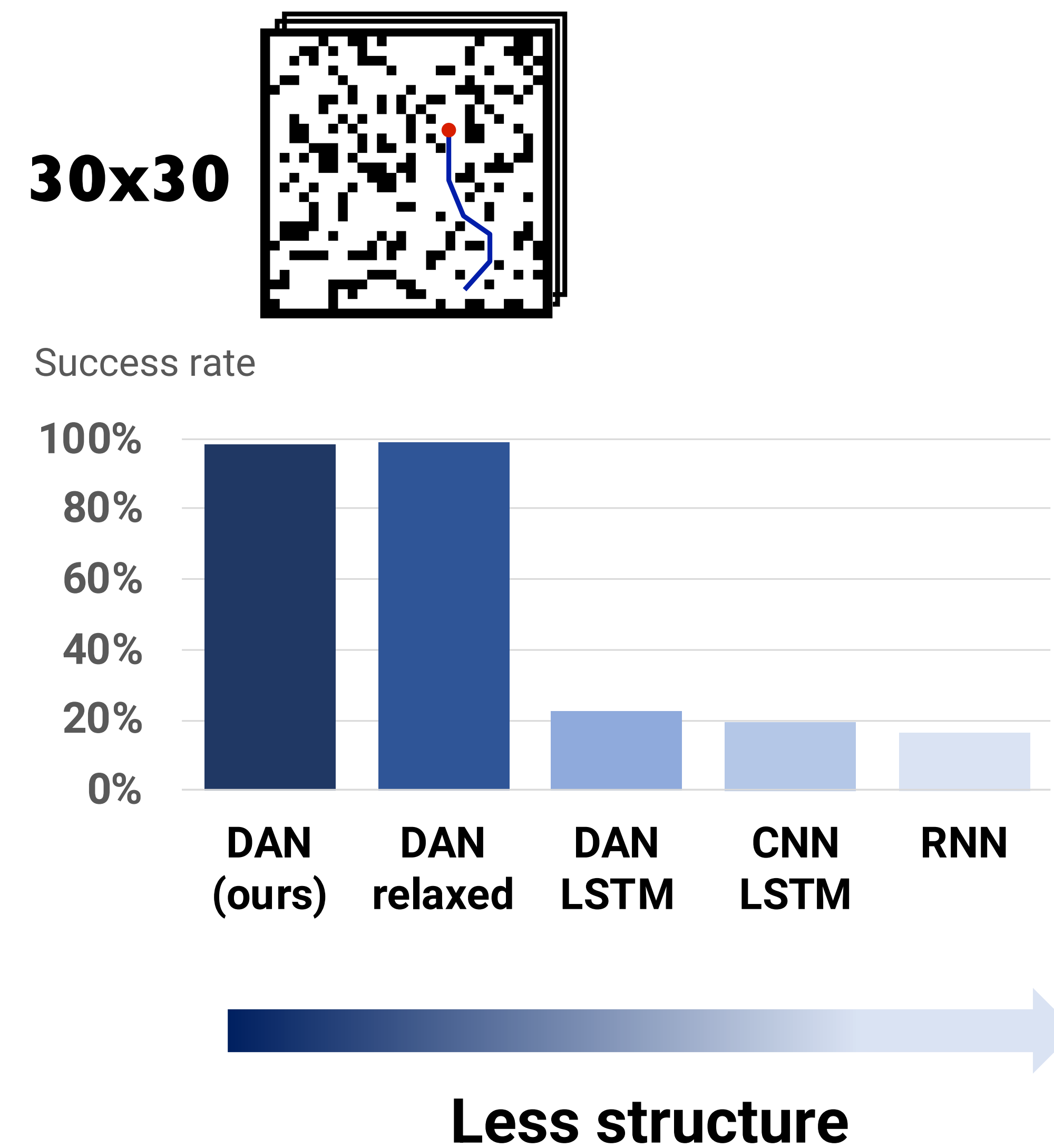
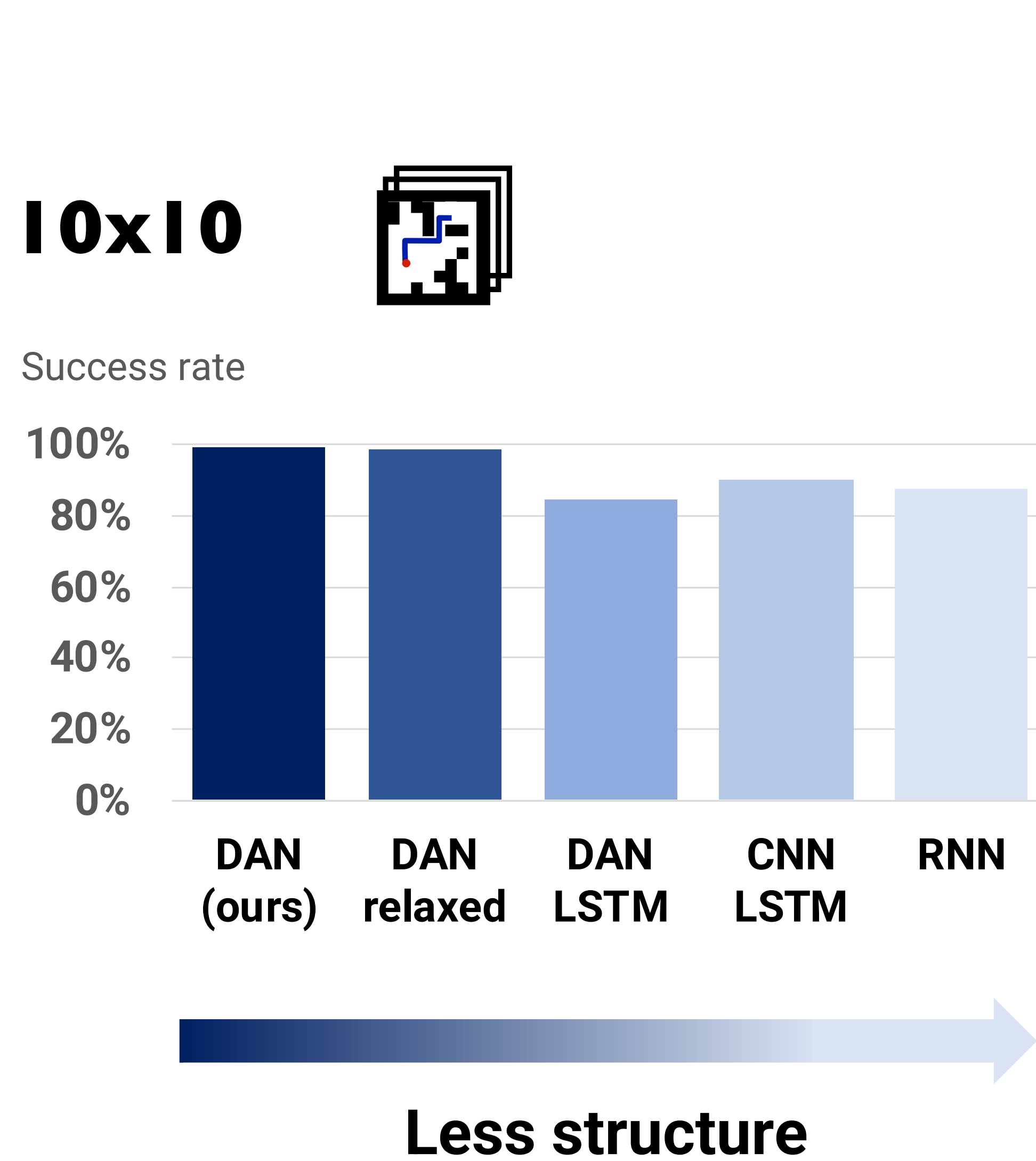


38.4%
success rate

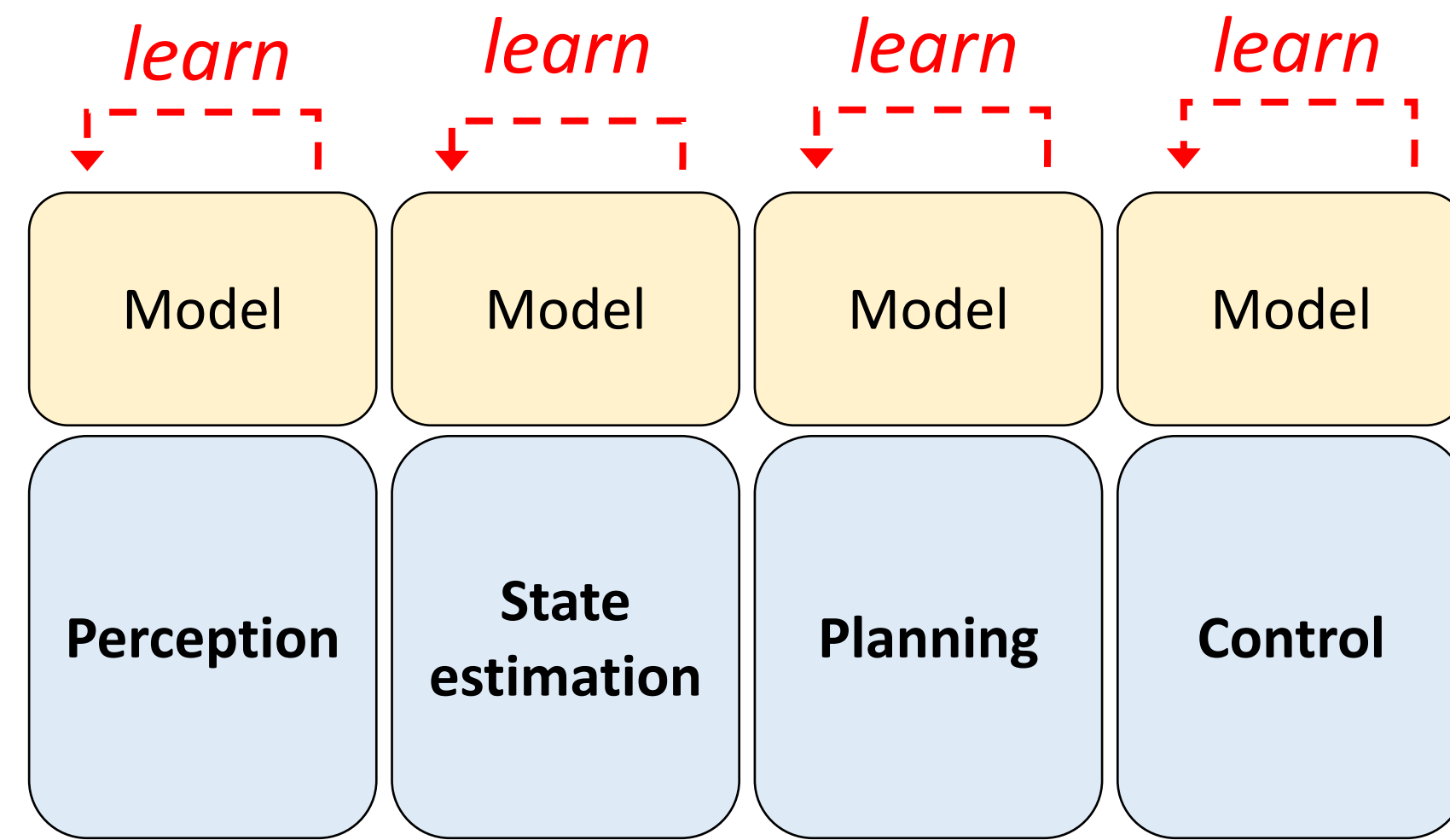


Structured prior

Structure priors help to generalize



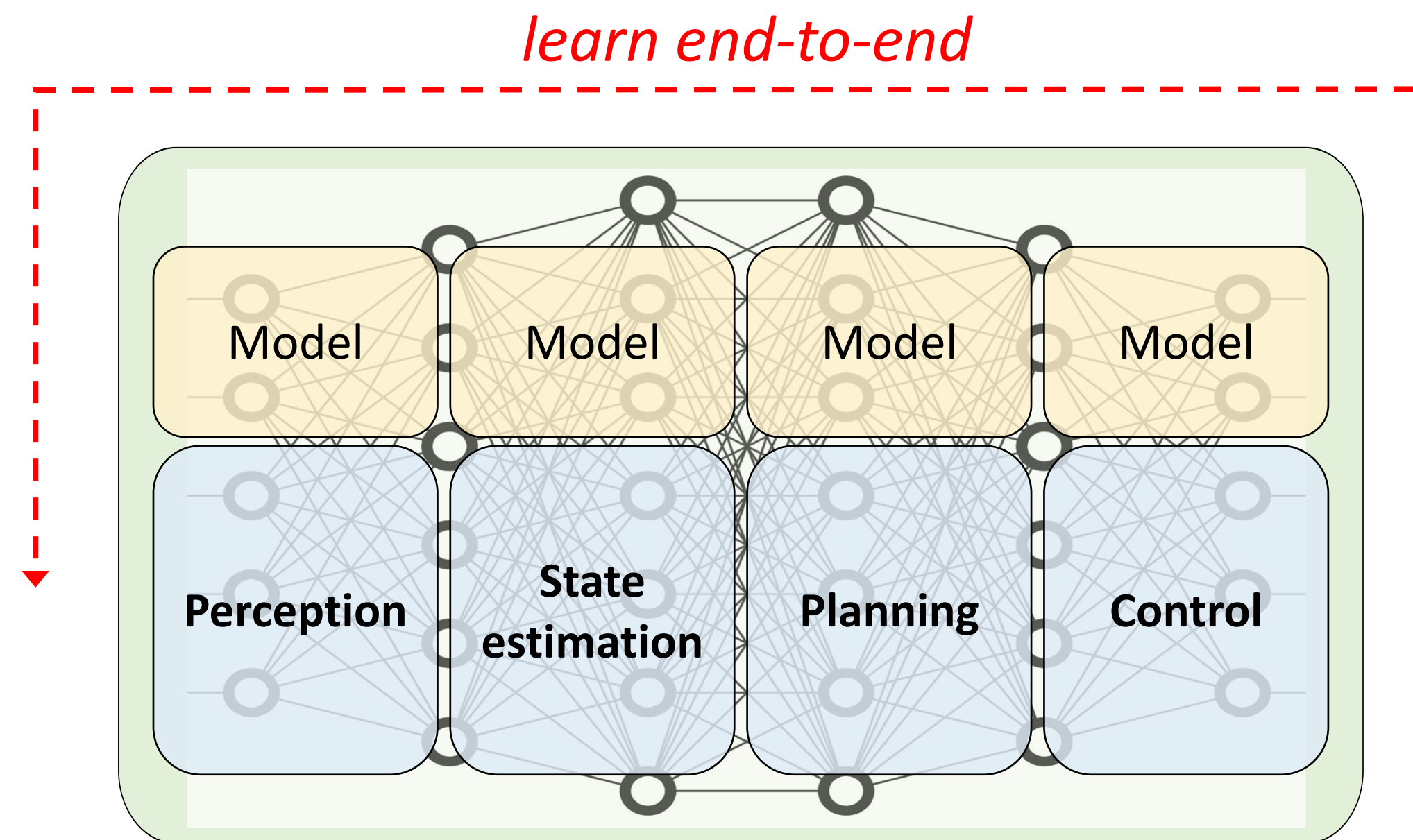
Modular



76.6%
success rate

Task-oriented learning

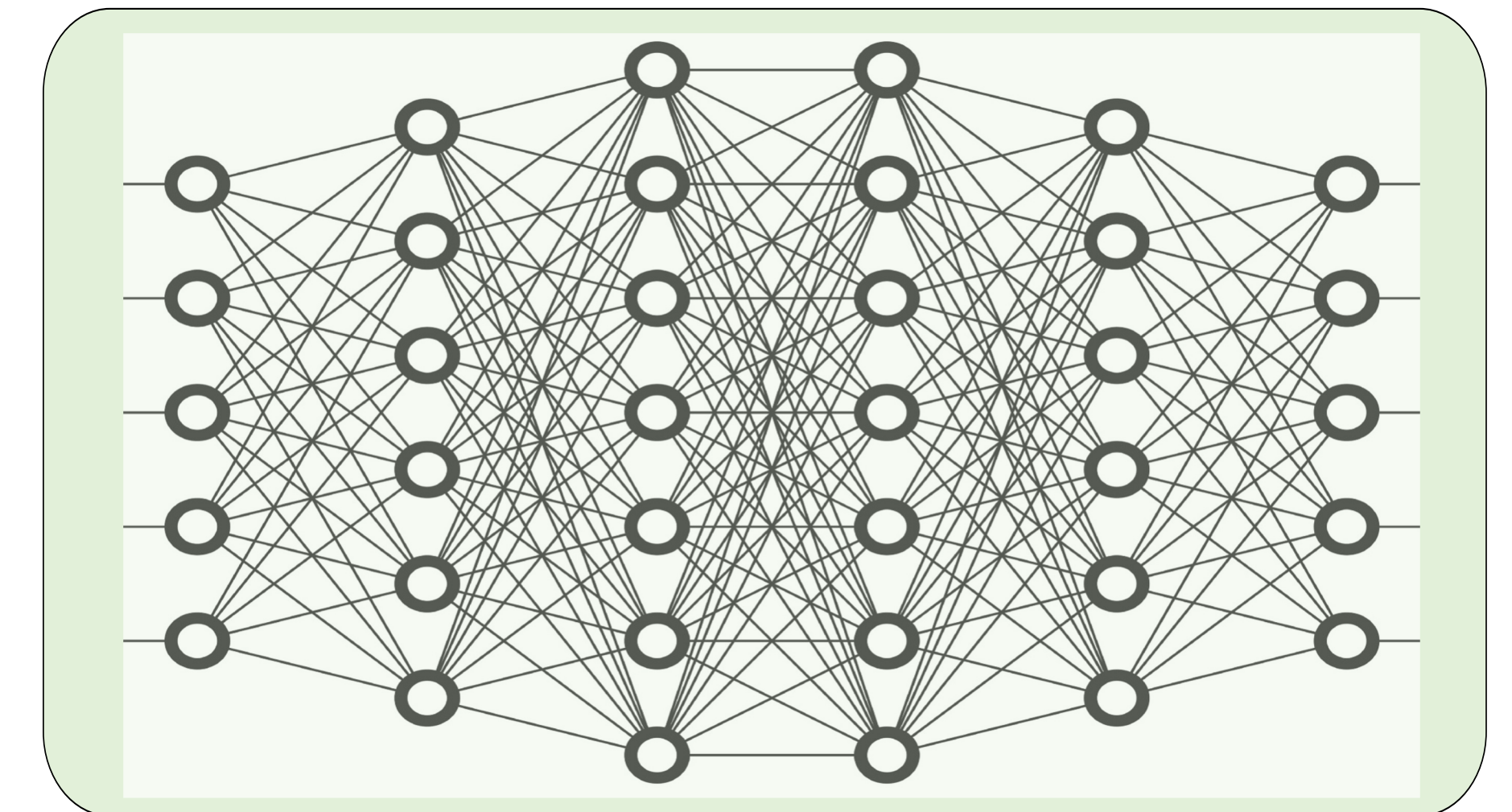
DAN (ours)



99.8%
success rate

Structure prior

End-to-end



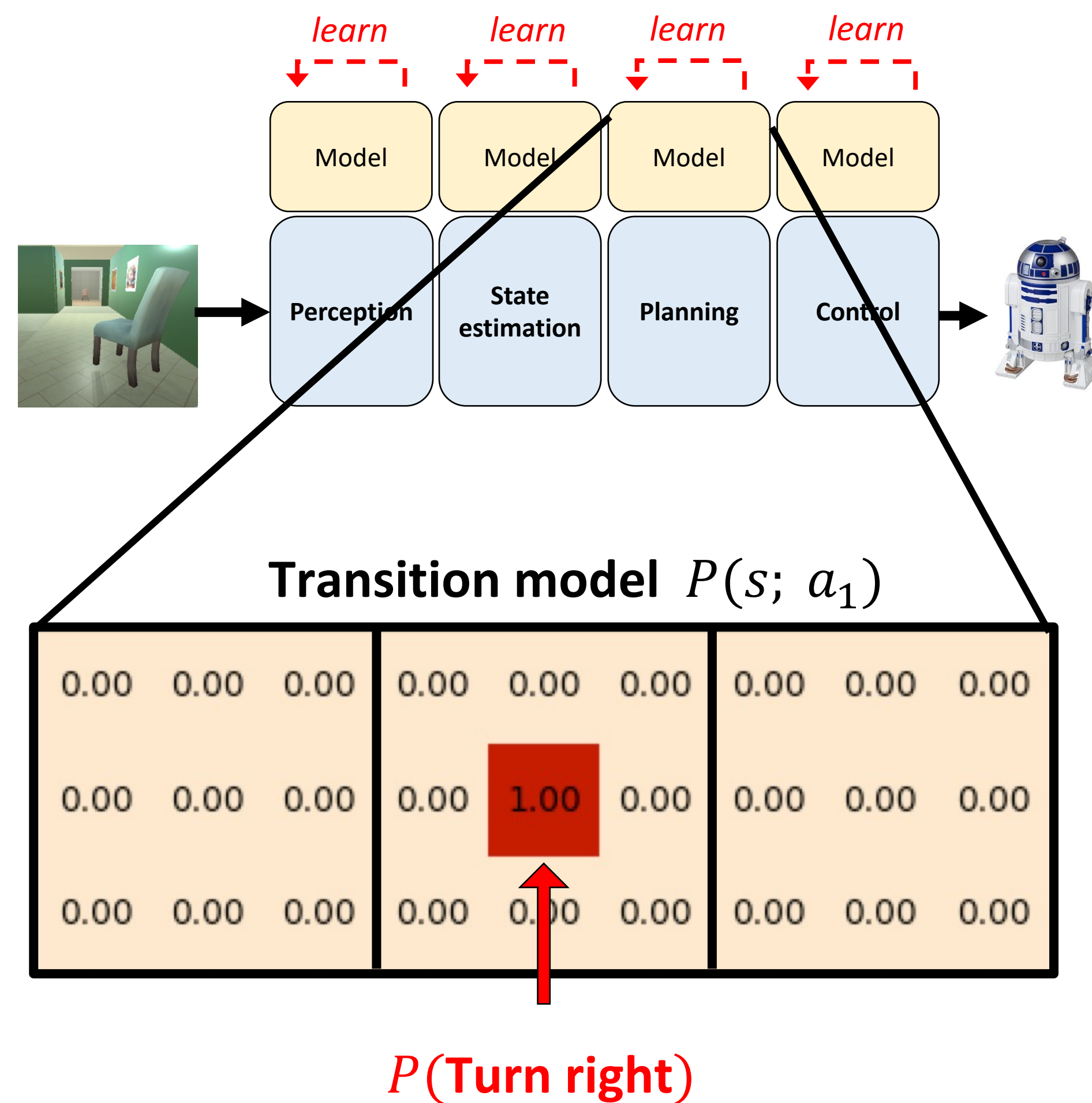
38.4%
success rate

A “wrong” model can fix a “wrong” algorithm

➤ Short planning horizon

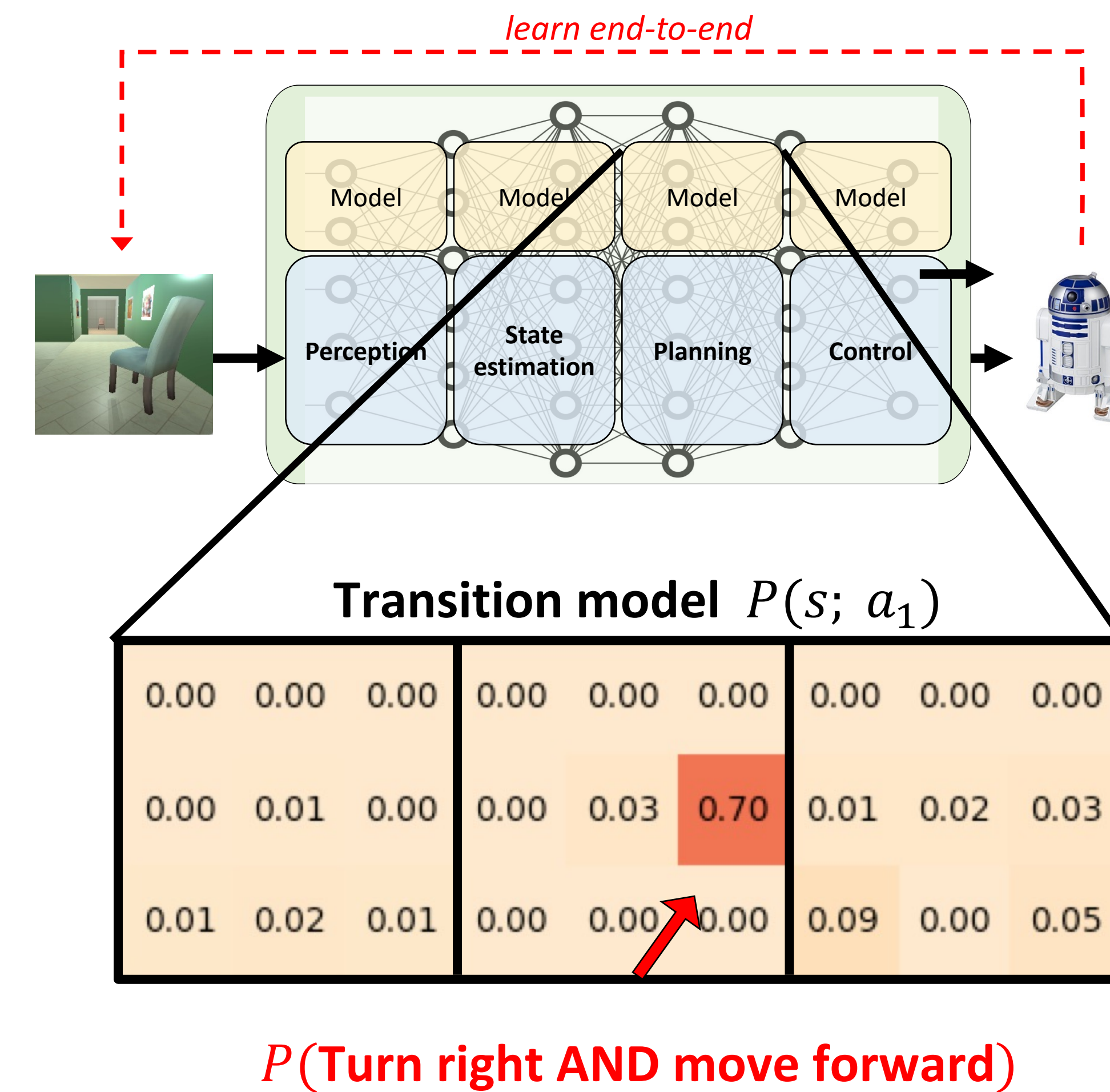
Model-based

59.0%
success rate



DAN (ours)

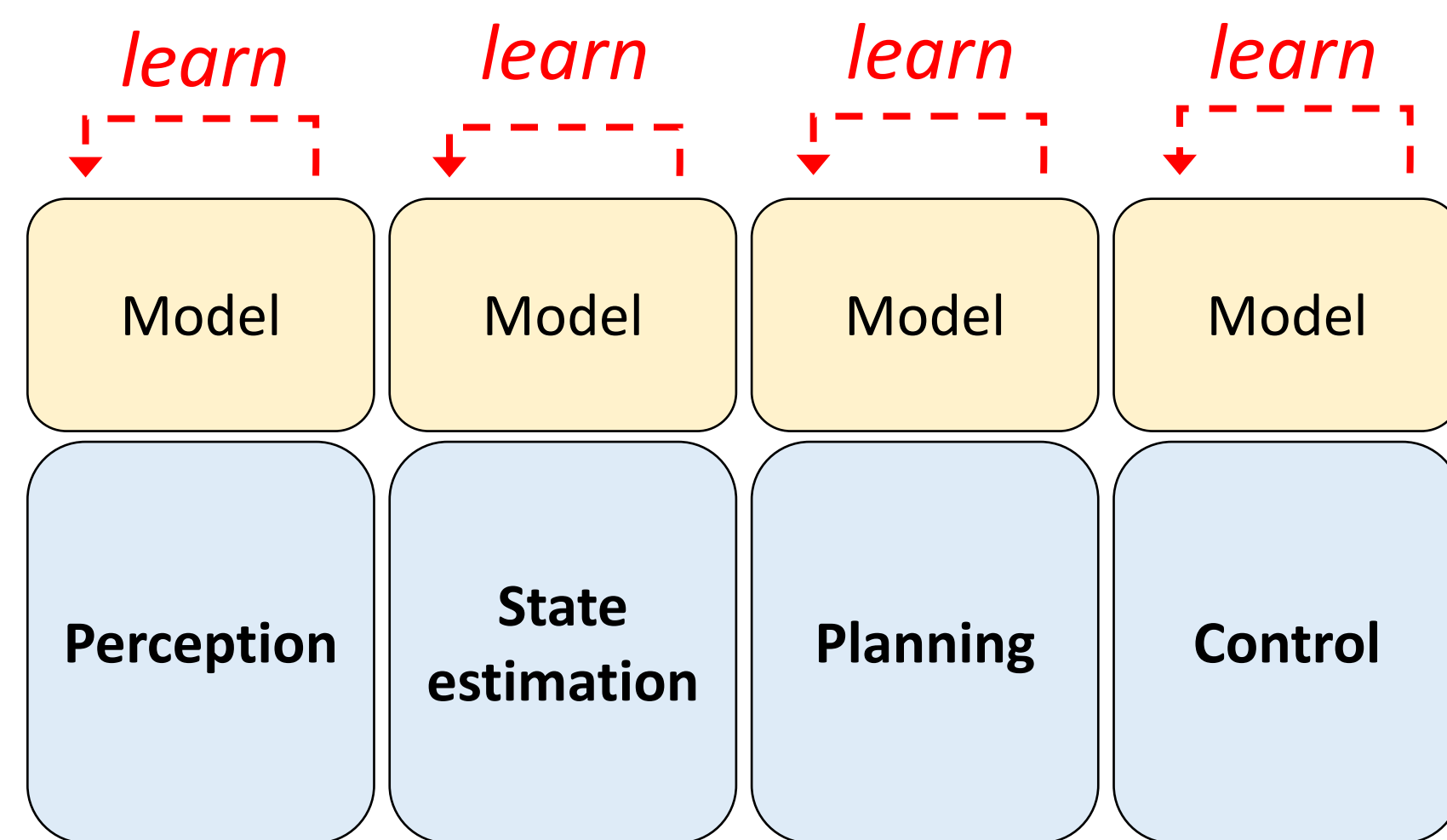
97.8%
success rate



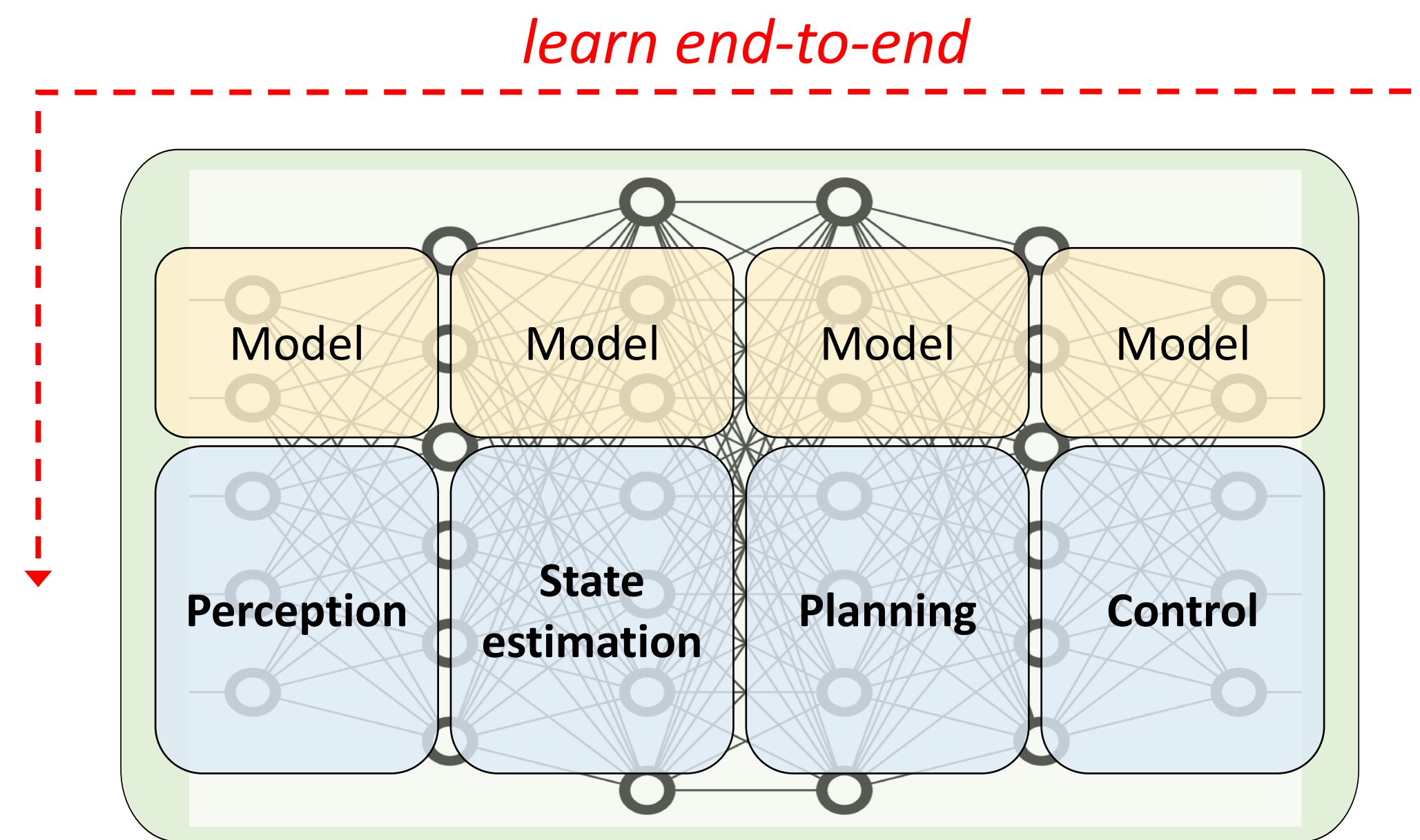
A “wrong” model can fix a “wrong” algorithm

- Short planning horizon? **Learn macro actions!**
- Transition model doesn't capture obstacles? **Learn to inflate collision penalties!**
- Cannot plan for information gathering? **Learn to reward it!**
- Perception mistakes lead to bad actions? **Learn to communicate confidence!**

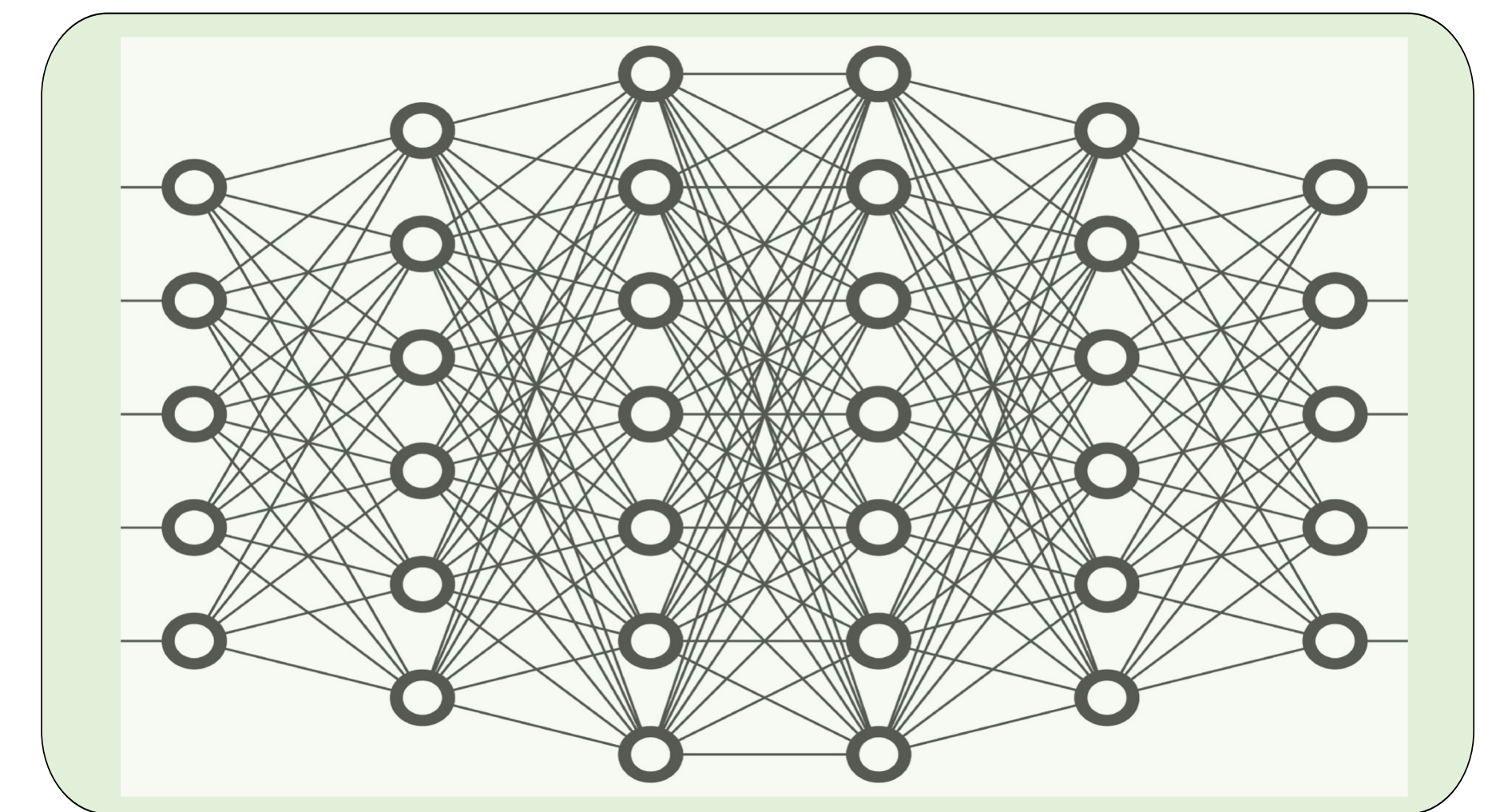
Modular



DAN

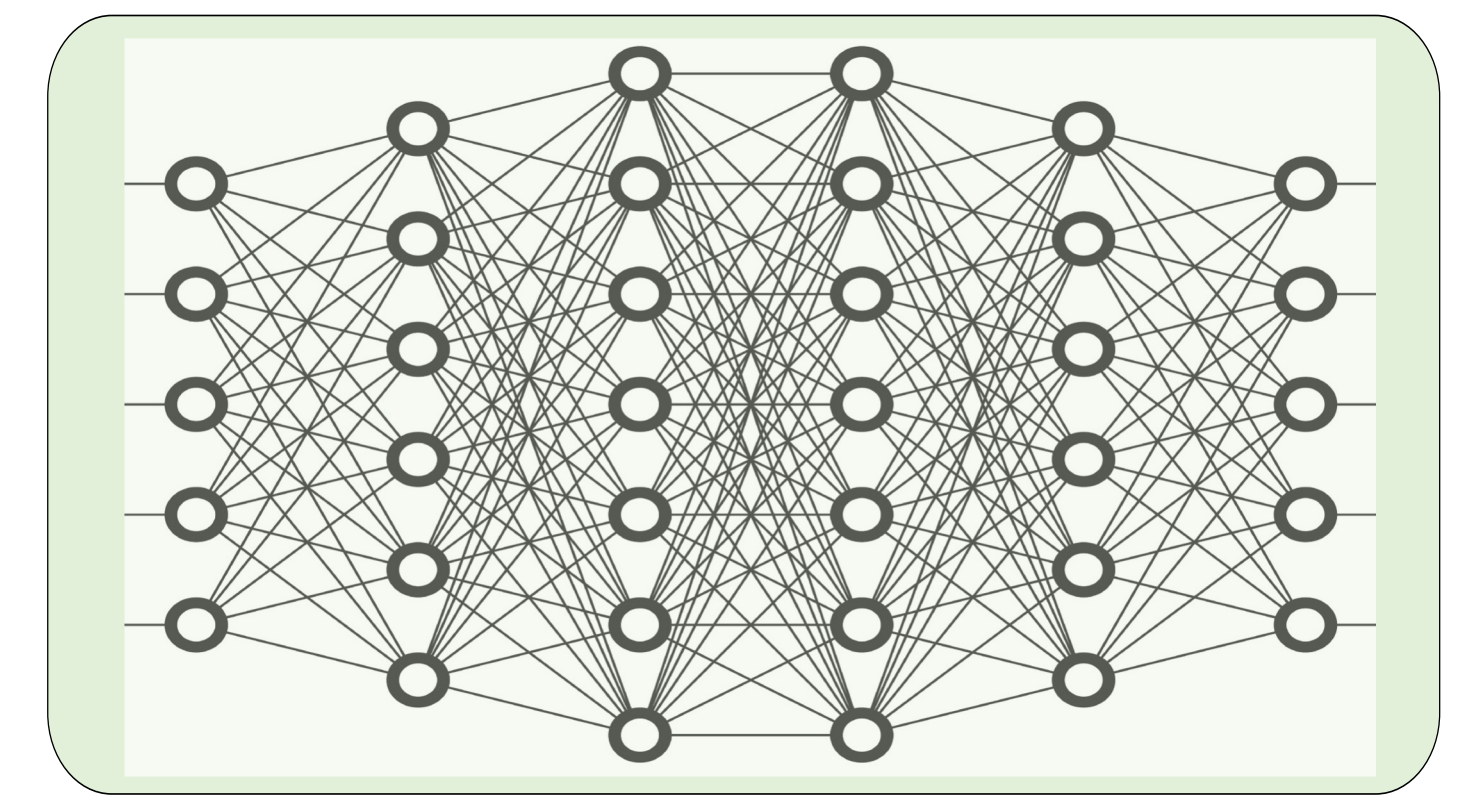
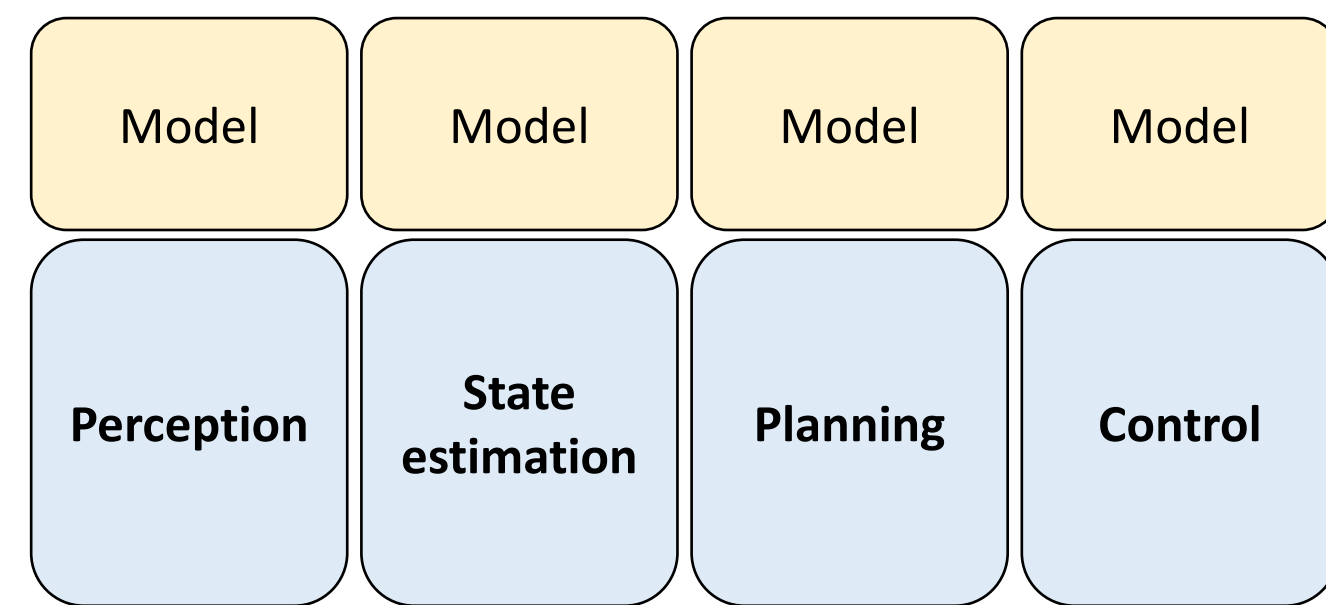


End-to-end



Task-oriented learning

Structure prior

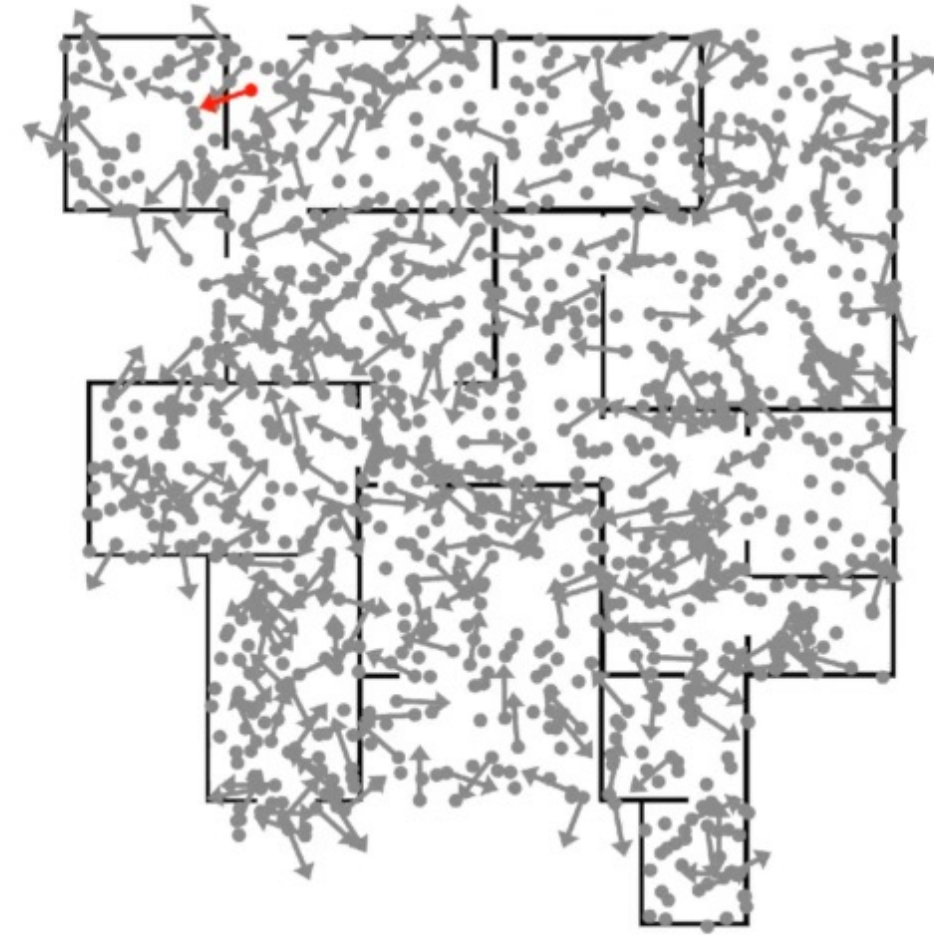


Model-based
algorithm
structure

DAN

Model-free
neural network

Applications



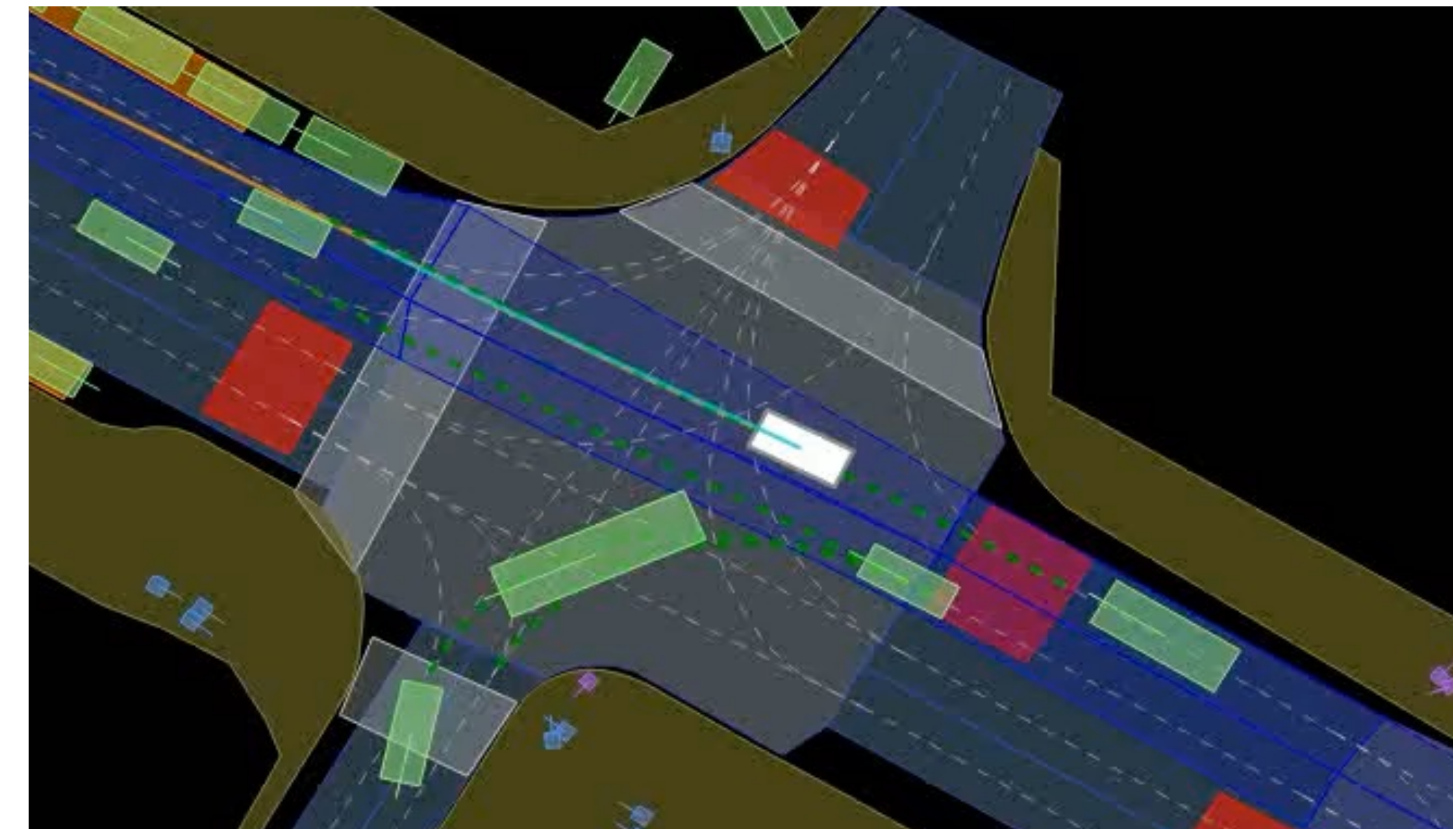
Visual localization



SLAM

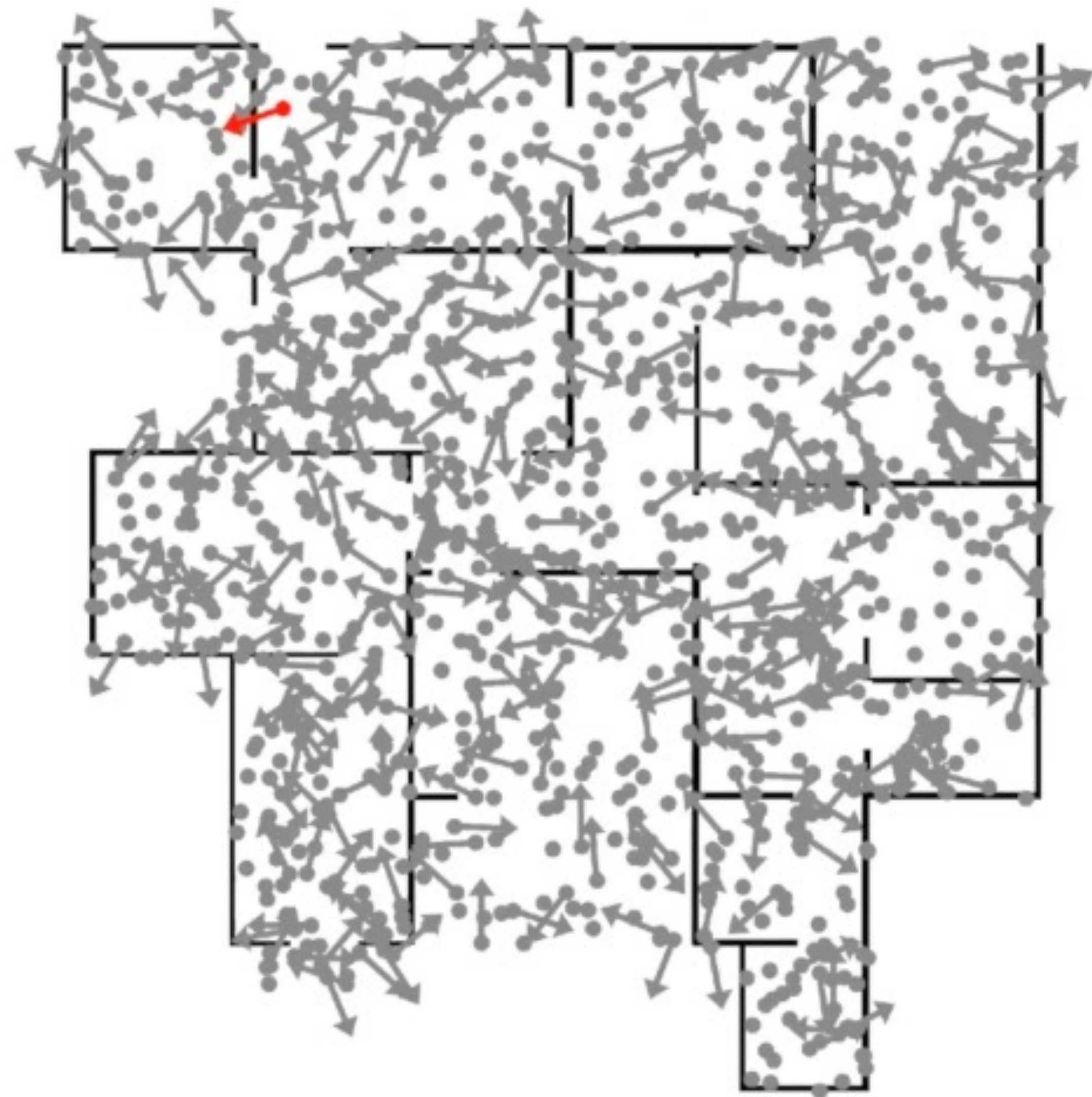


Navigation



Autonomous driving

Particle Filter Network

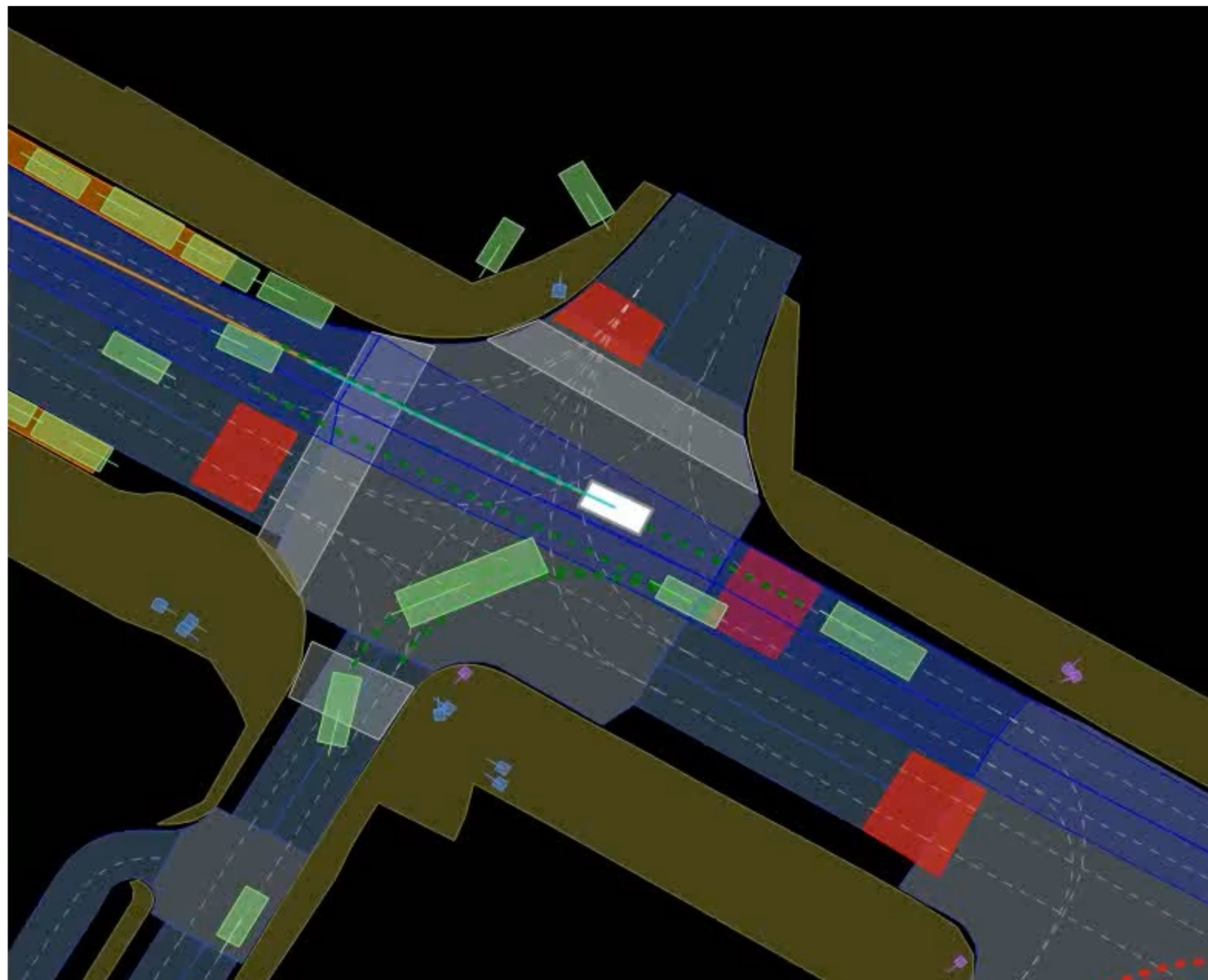


Differentiable SLAM-net

Spot navigation demo

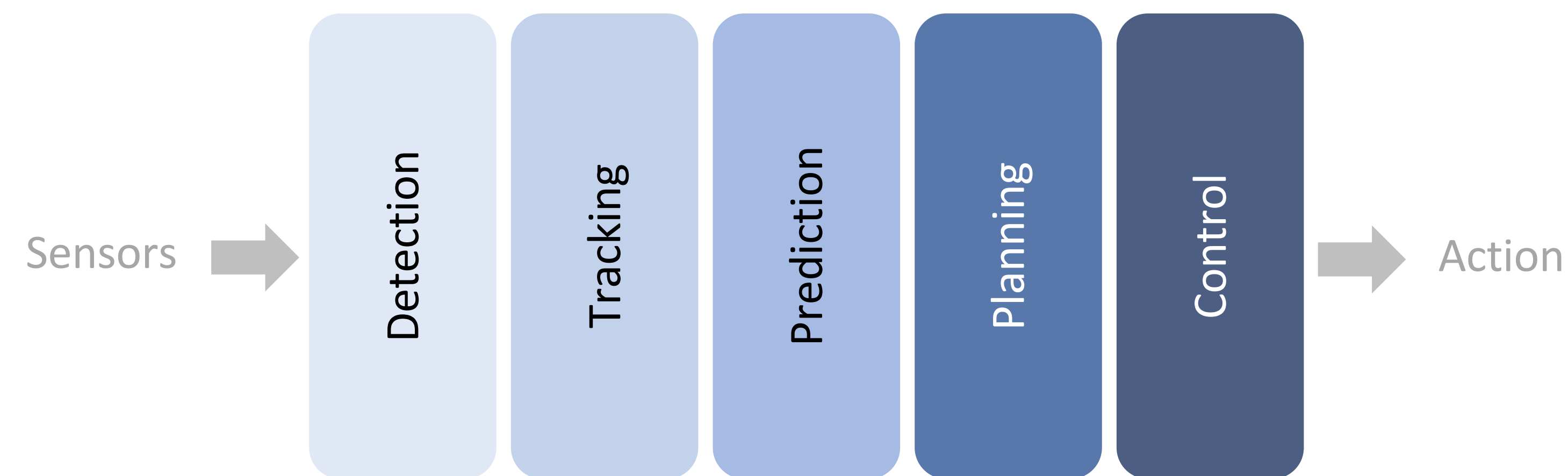


Autonomous driving

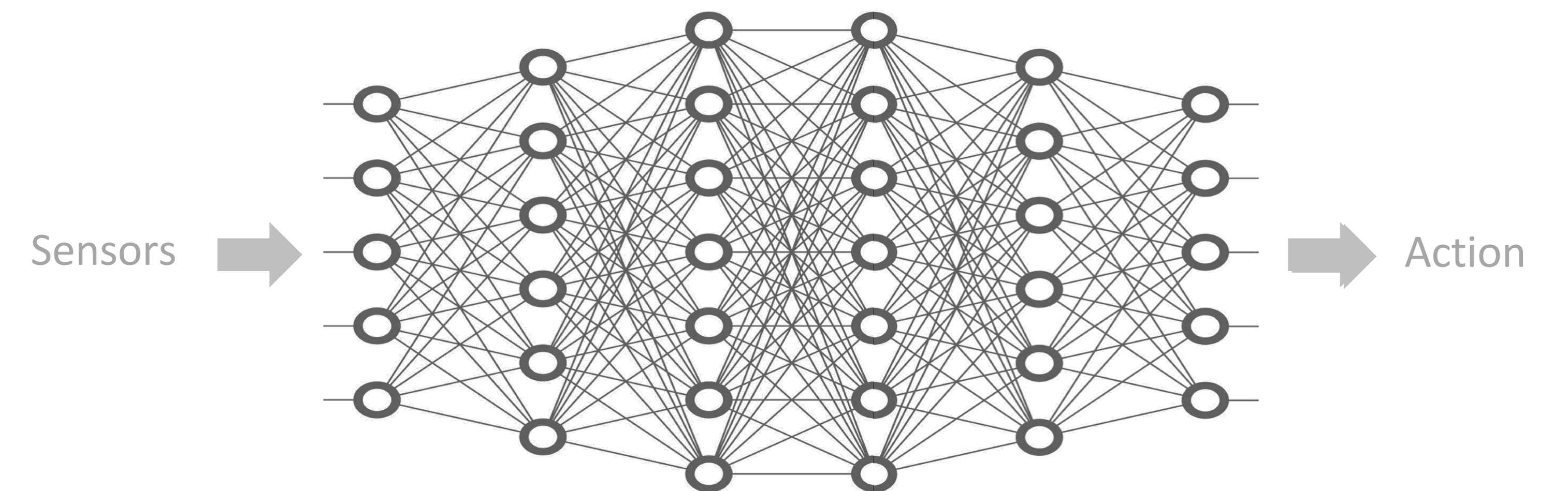


Differentiable & Modular AV Stacks

Motivation



Modular architecture

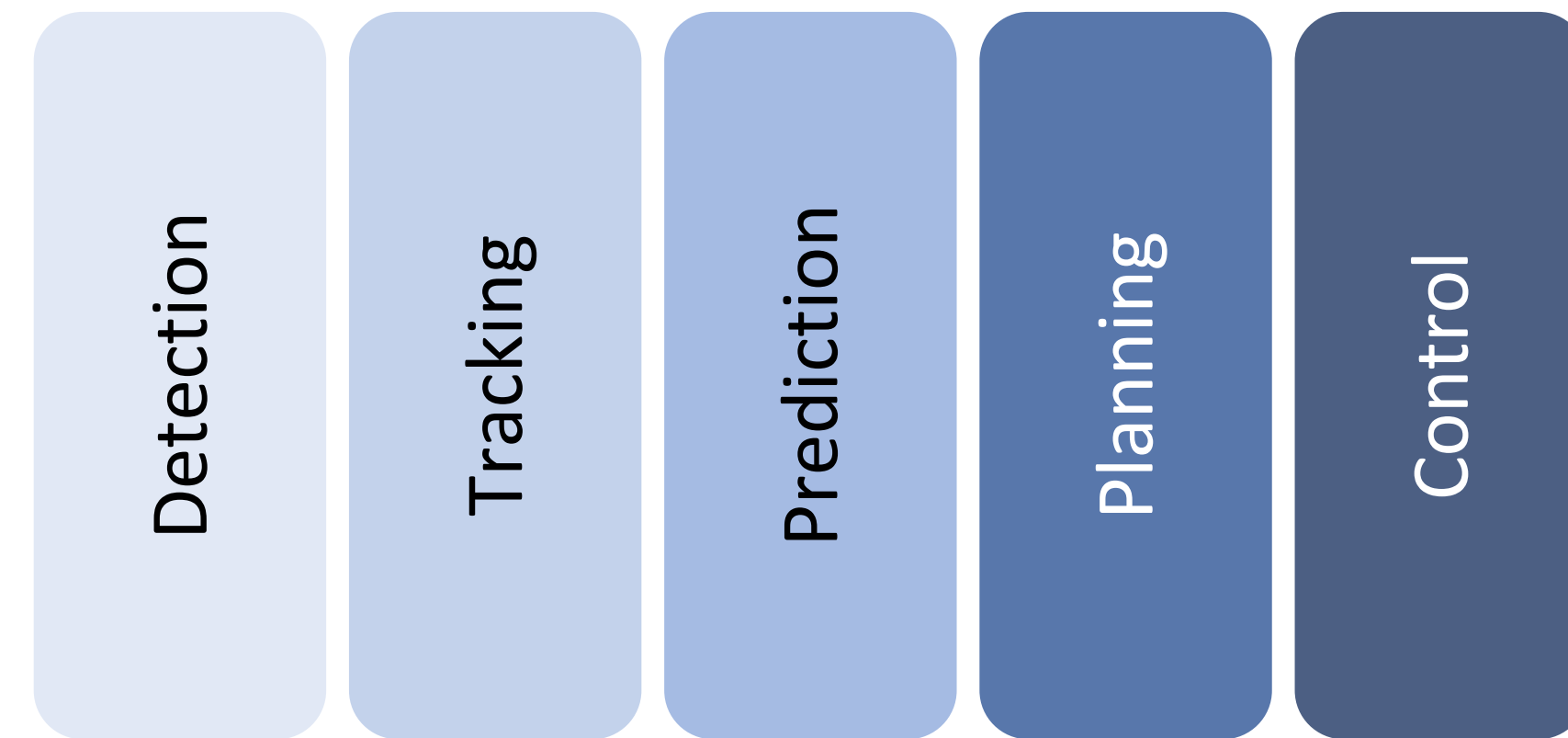


End-to-end architecture

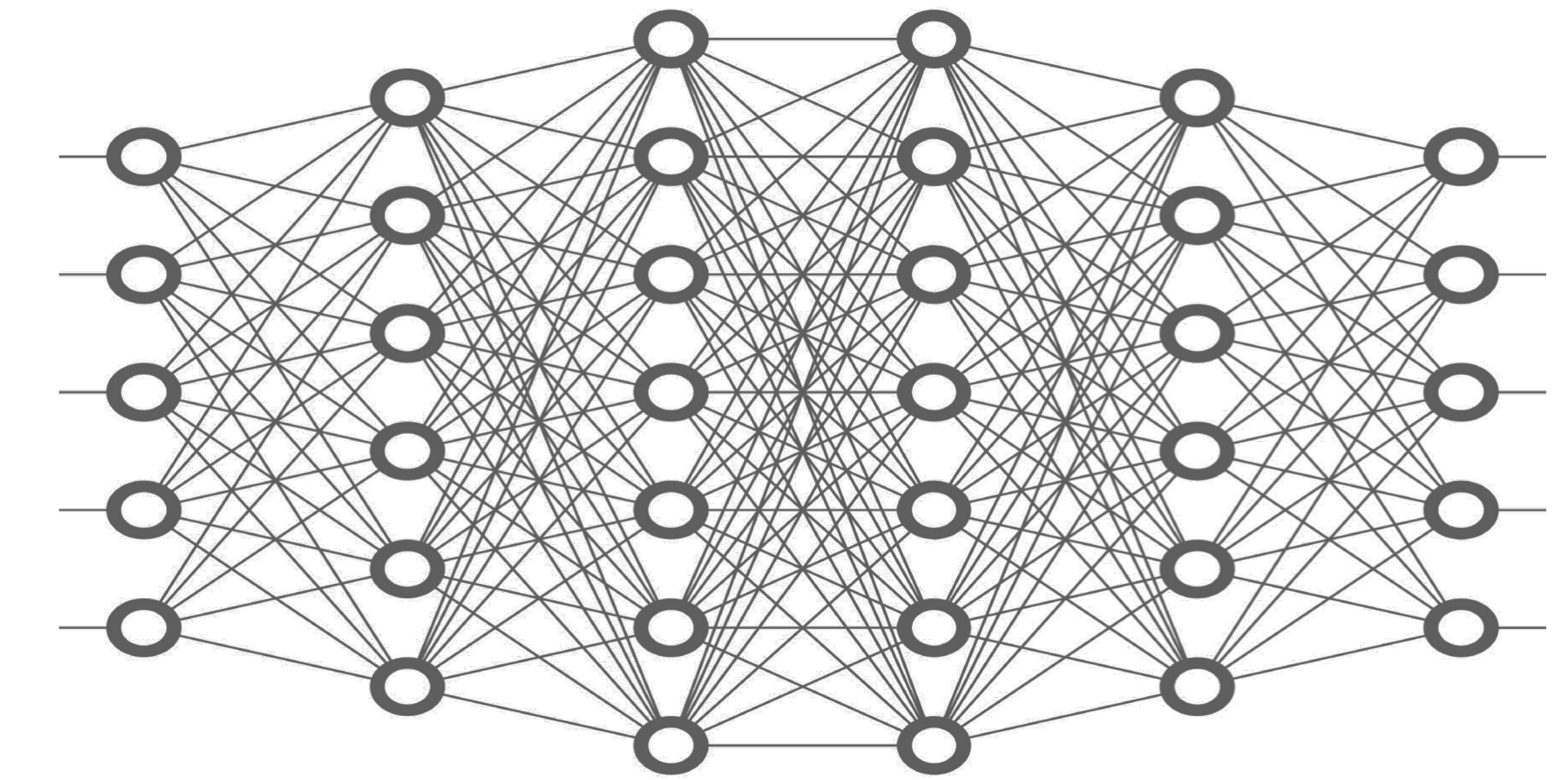
?

Differentiable & Modular AV Stacks

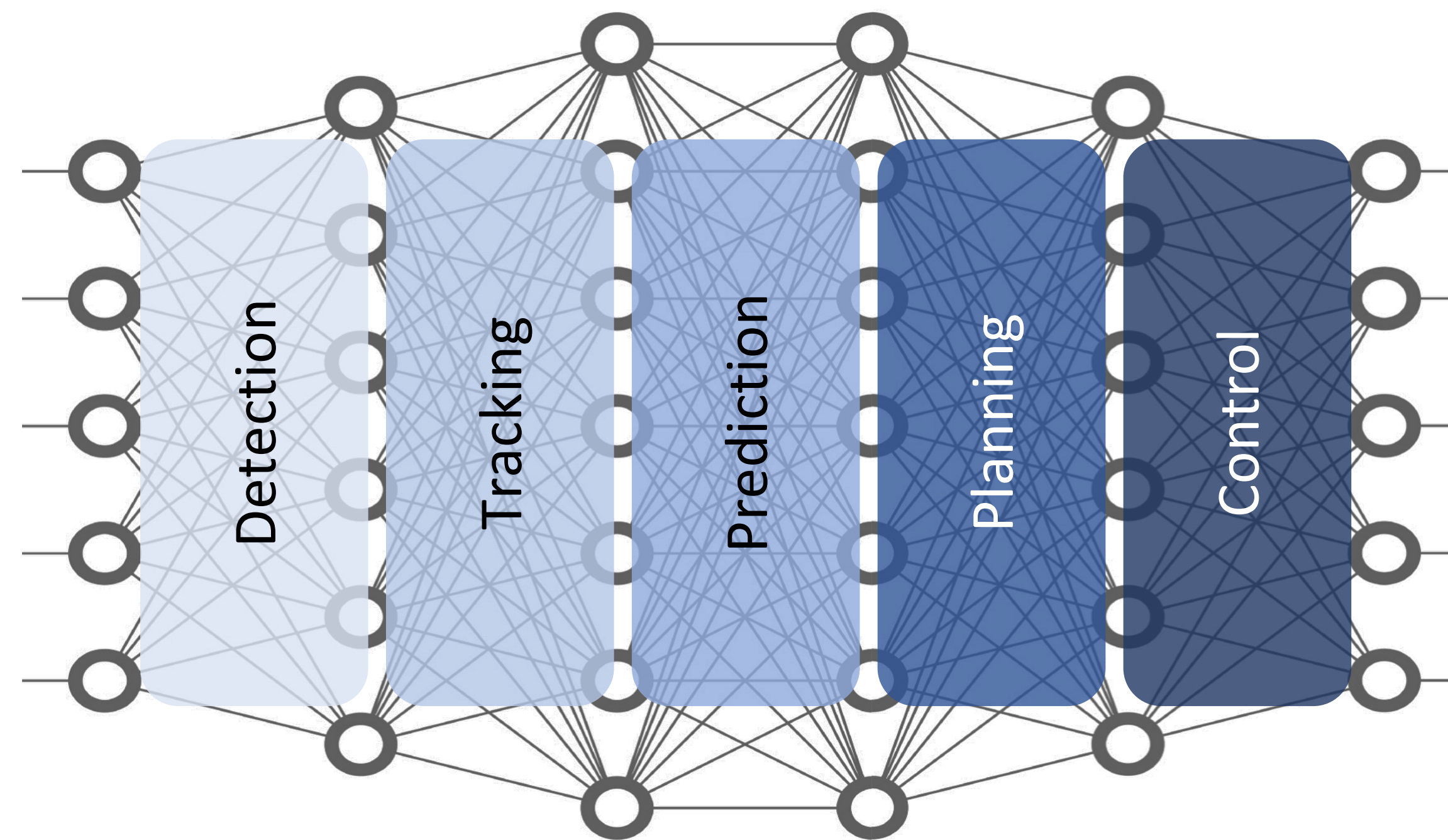
Key idea



Modular architecture



End-to-end architecture

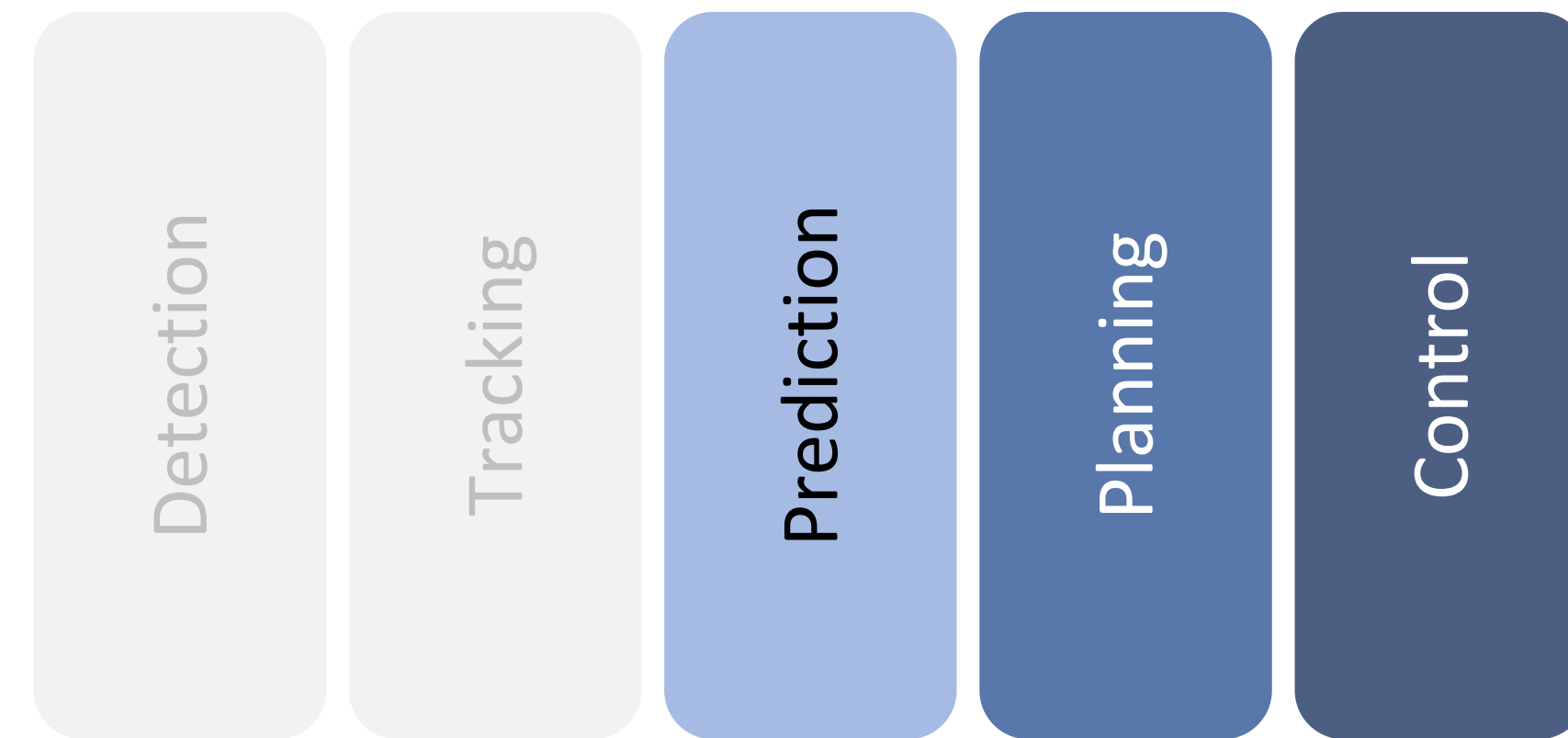


Differentiable & modular stack

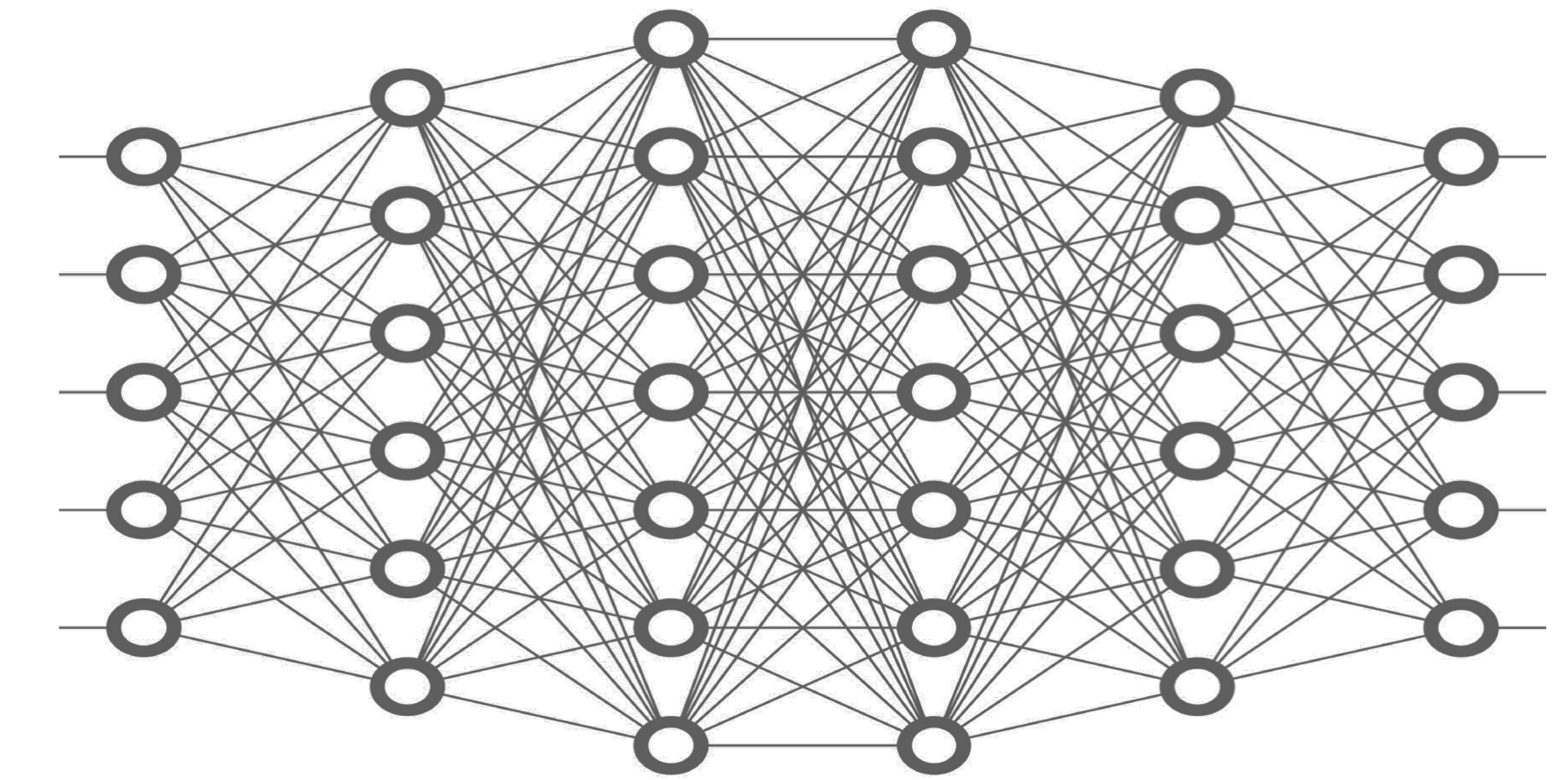
Idea: use a differentiable computation graph to represent modules and train them end-to-end

Differentiable & Modular AV Stacks

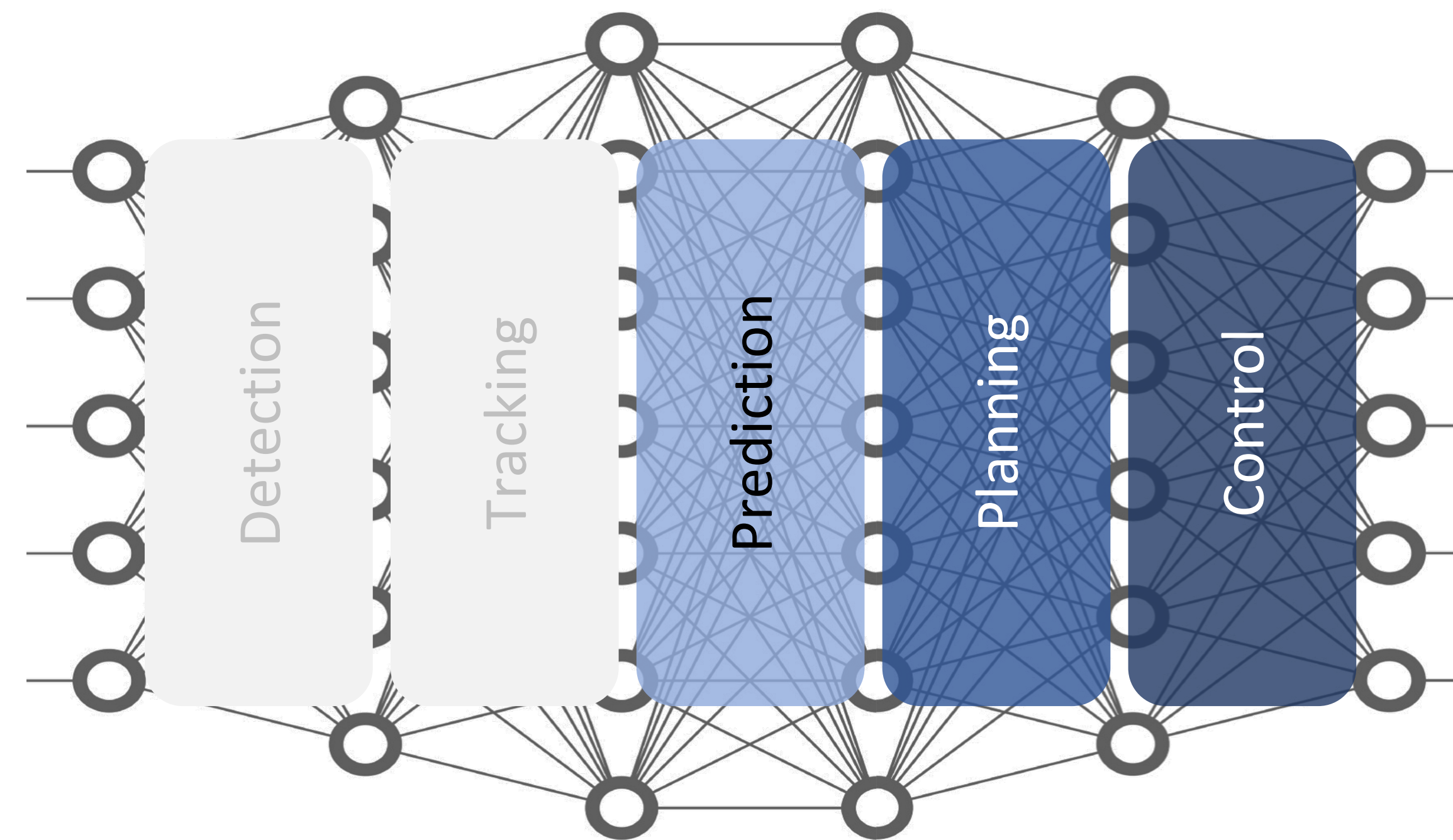
Example



Modular architecture

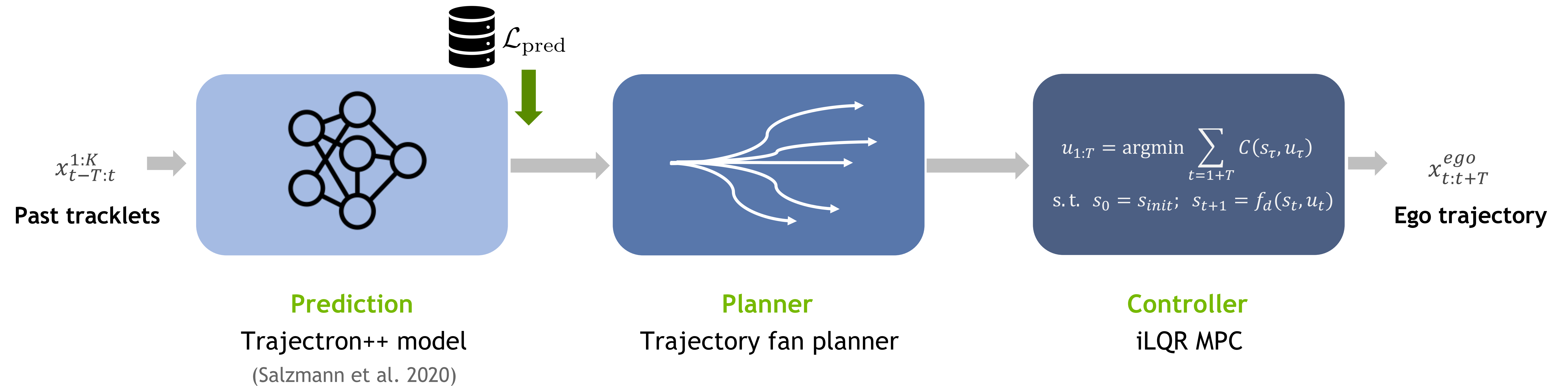


End-to-end architecture

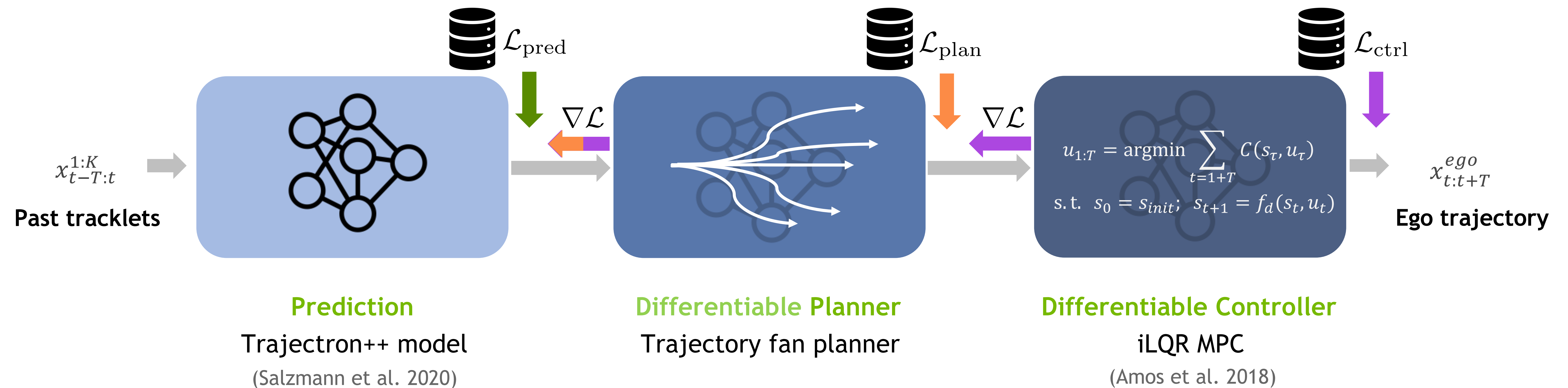


Differentiable & modular stack

DIFFSTACK: DIFFERENTIABLE PREDICTION-PLANNING-CONTROL

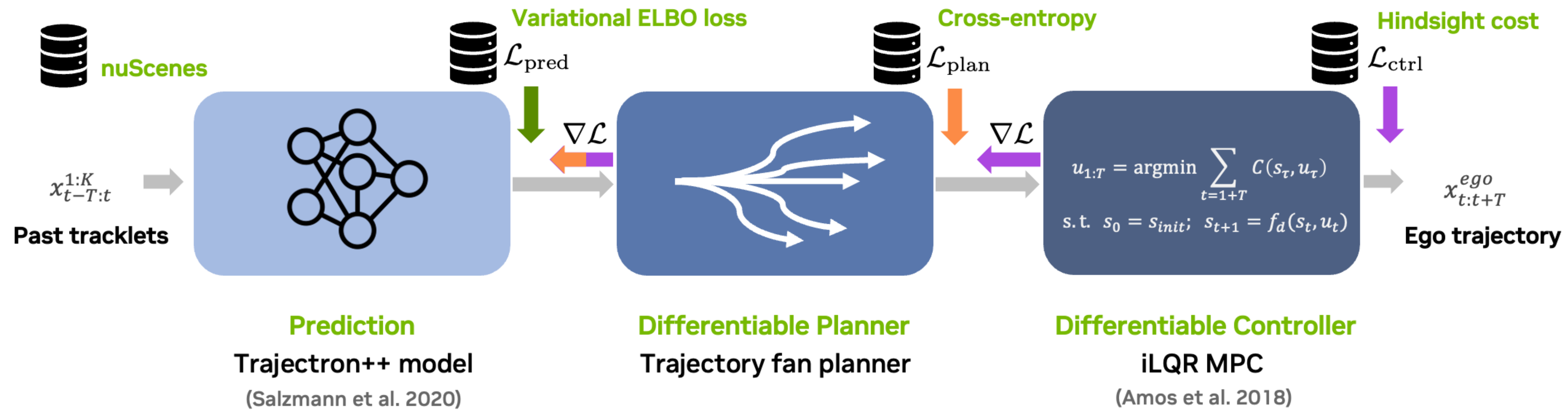


DIFFSTACK: DIFFERENTIABLE PREDICTION-PLANNING-CONTROL



Differentiable & Modular AV Stacks

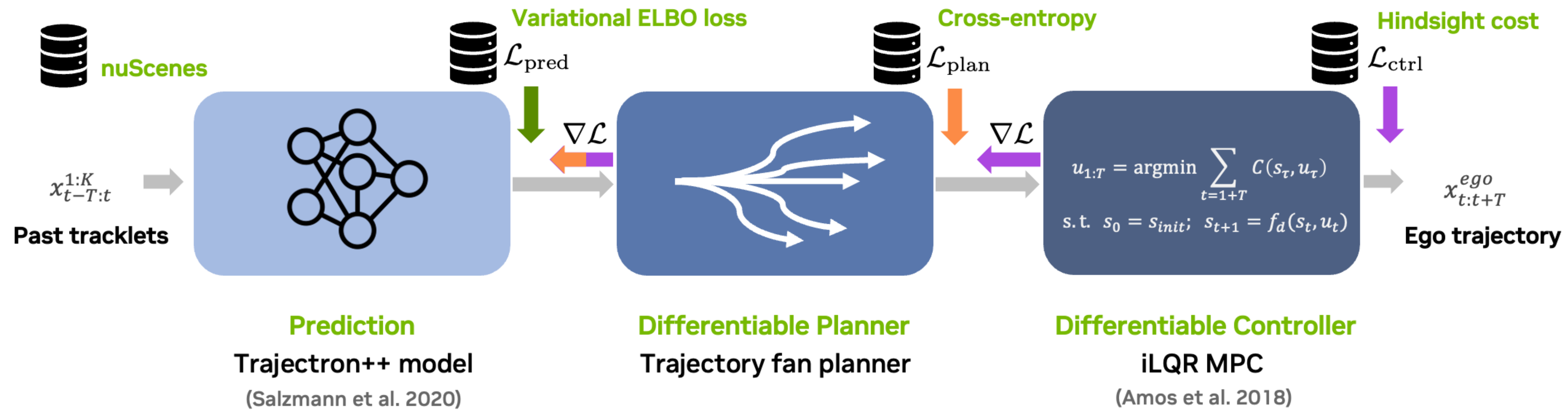
Quantitative results



Standard modular stack		
Differentiable stack (ours)		

Differentiable & Modular AV Stacks

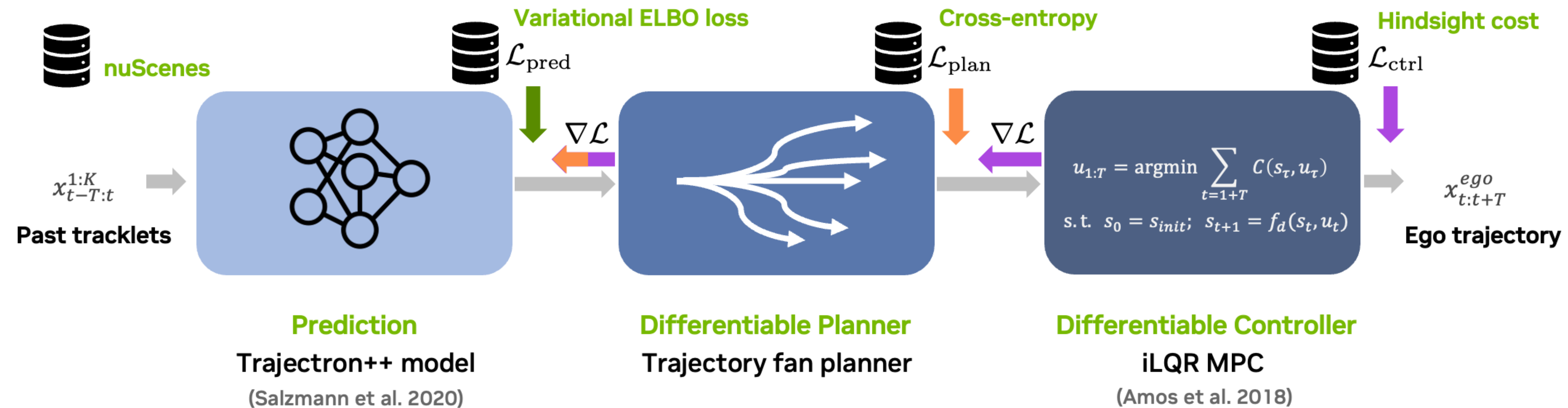
Quantitative results



	Perception performance ADE (m) ↓	
Standard modular stack	1.32 ± 0.06	
Differentiable stack (ours)	1.27 ± 0.07	

Differentiable & Modular AV Stacks

Quantitative results



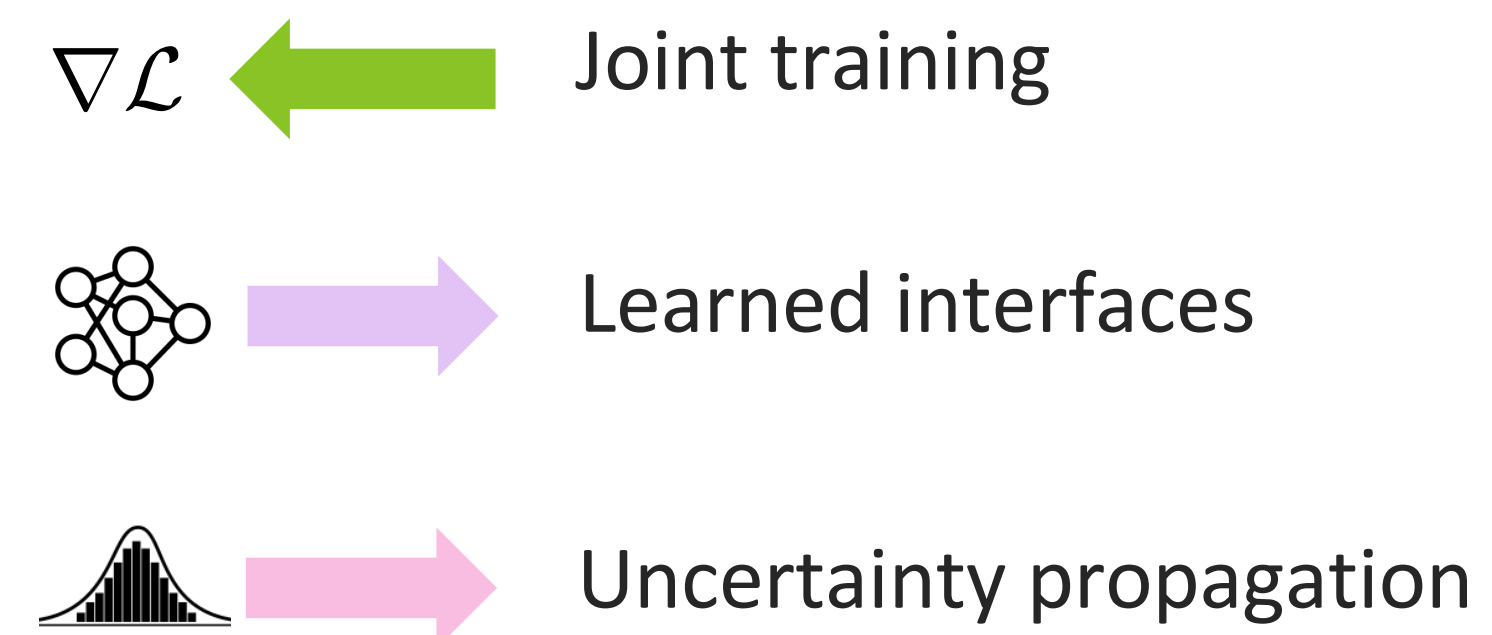
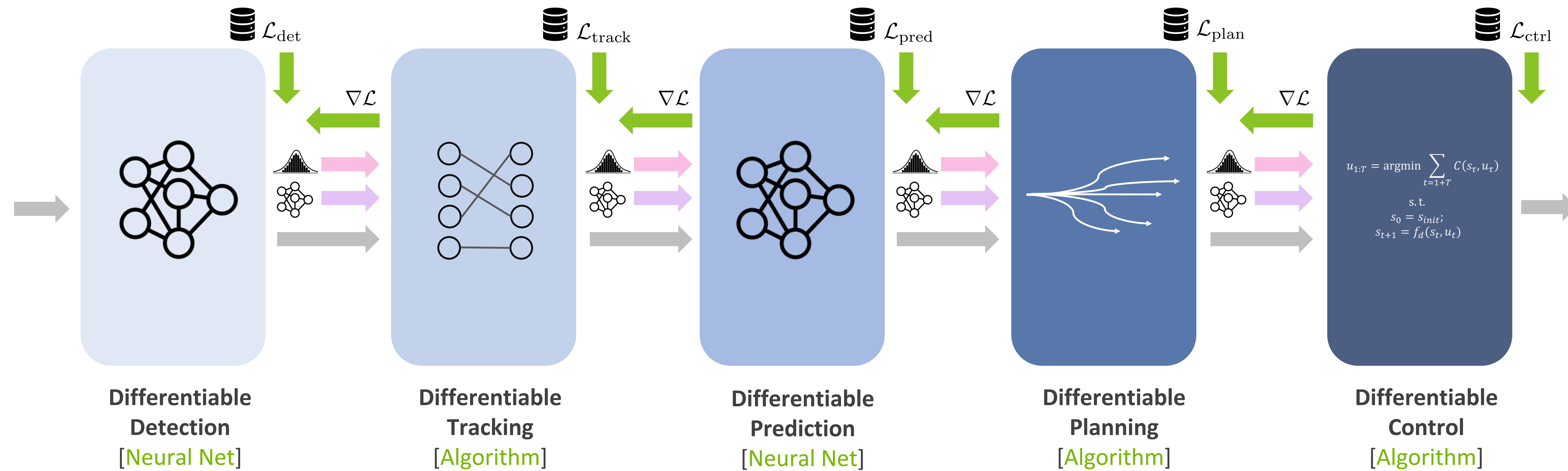
	Perception performance ADE (m) ↓	Cost difference from theoretical best ↓
Standard modular stack	1.32 ± 0.06	29% ± 2%
Differentiable stack (ours)	1.27 ± 0.07	17% ± 2%

Upper bound on cost: planning with no predictions

Lower bound on cost: planning with ground truth predictions

Differentiable & Modular AV Stacks

Vision



- ✓ Adversarial robustness & safety
- 📊 Task-oriented metrics
- 🗄️ Simulation technology

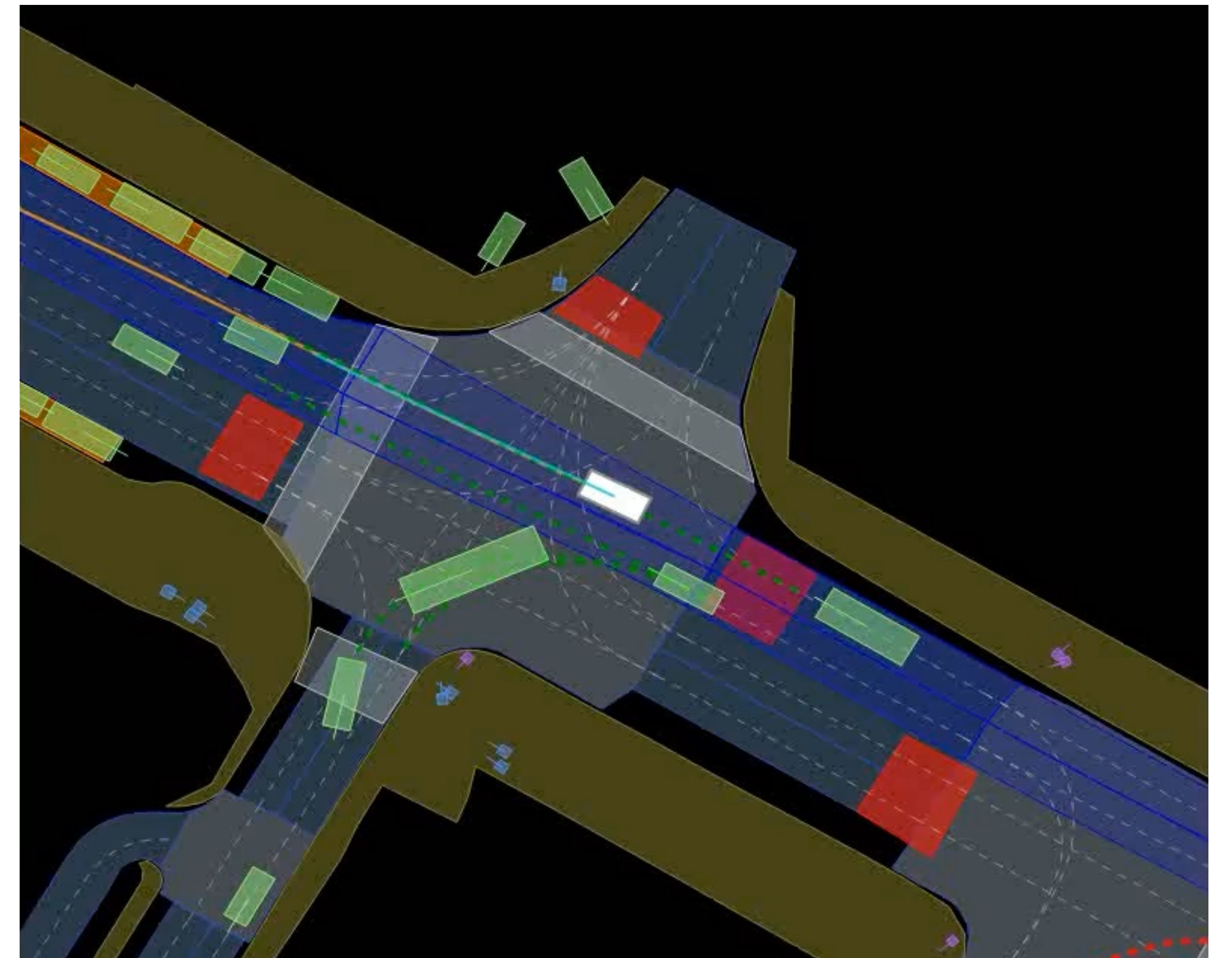
Differentiable & Modular AV Stacks

Ongoing work

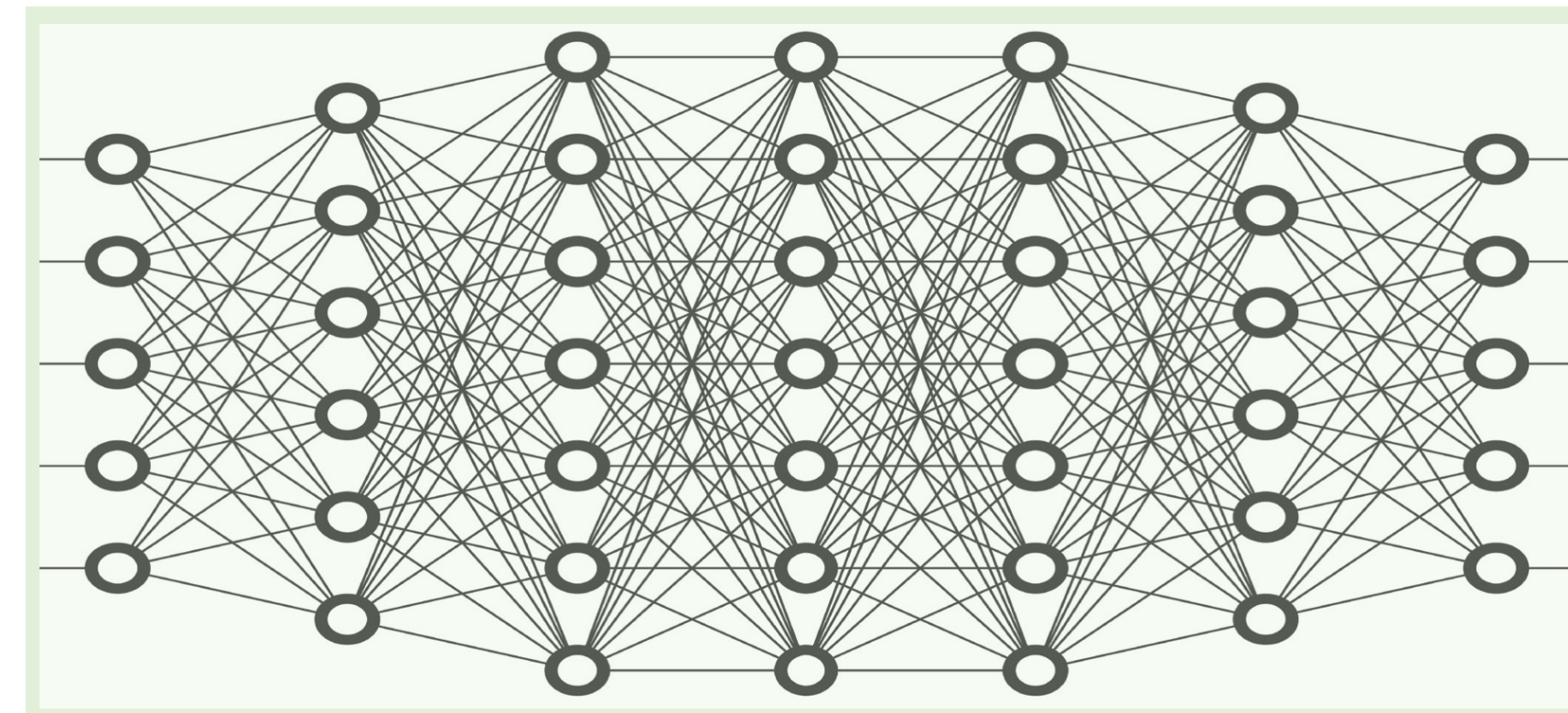
CARLA Driving Challenge



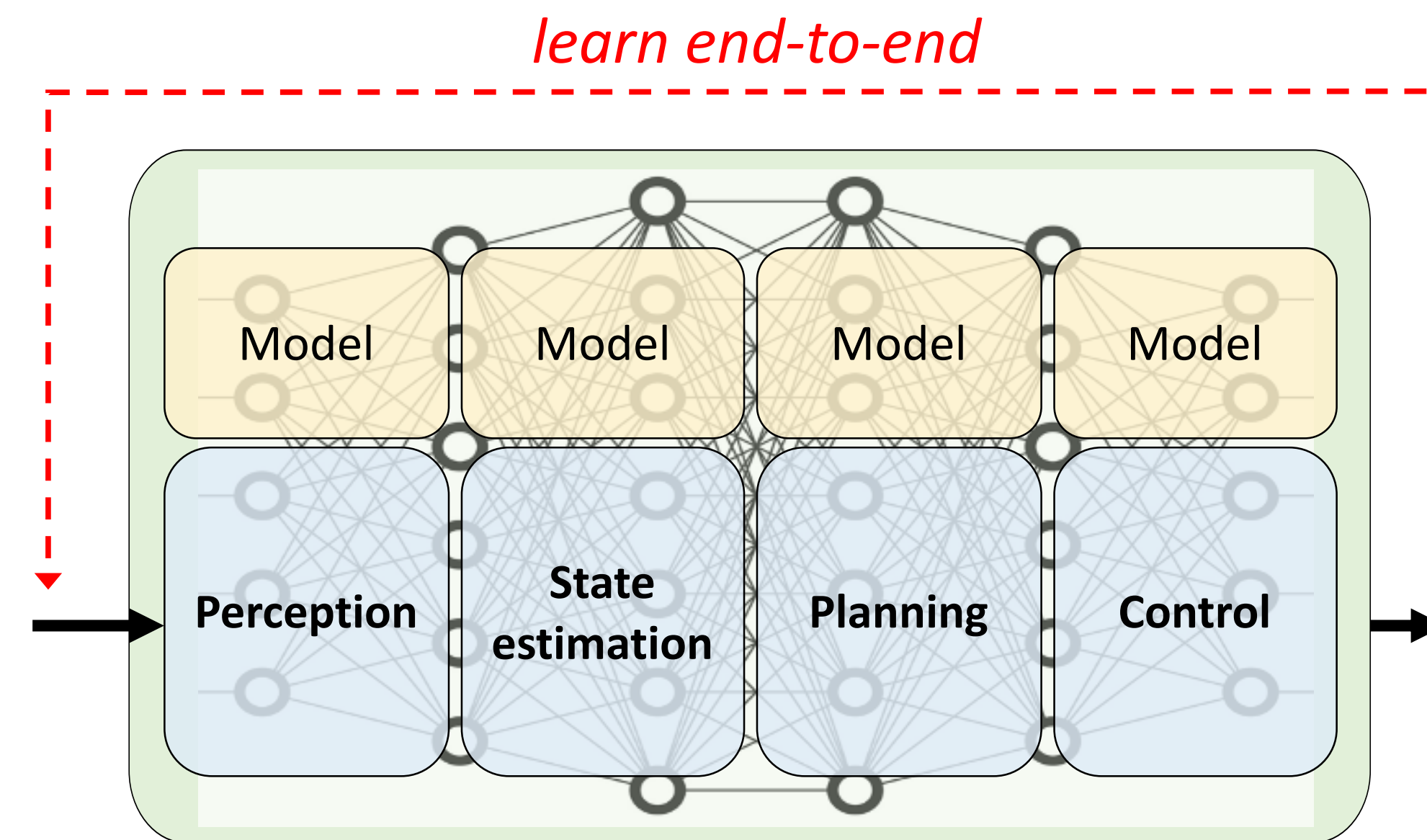
nuPlan Driving Challenge



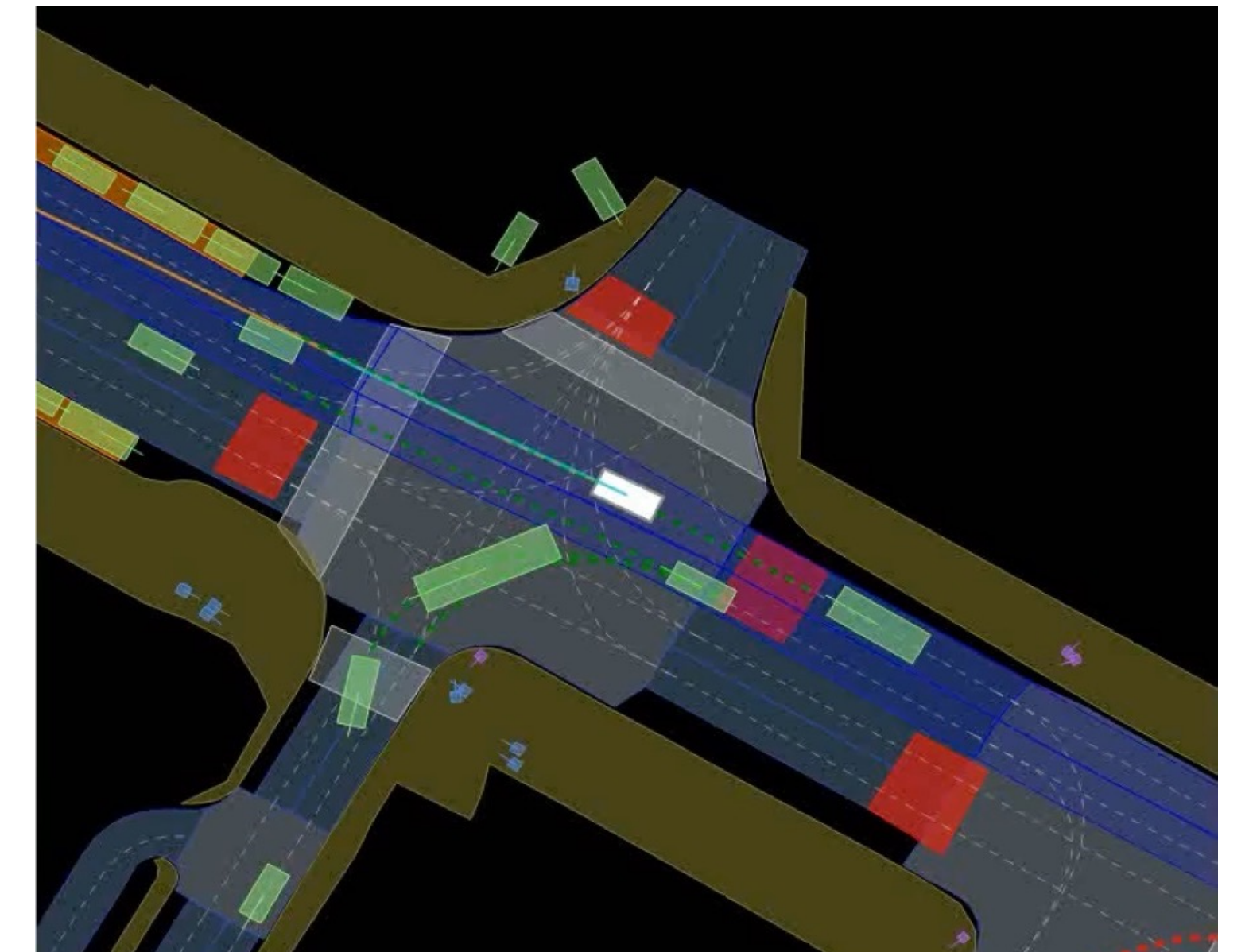
Summary



Algorithms can be built into neural networks



DAN =
Modular + Task-oriented



Applications